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PRELIMINARY REPORT ON  
FIRE HAZARD RATING STUDY

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# THE HISTORY OF THE UNITED STATES OF AMERICA

## FROM 1789 TO 1861

The history of the United States of America from 1789 to 1861 is a story of growth, struggle, and transformation. It begins with the signing of the Declaration of Independence in 1776, which marked the birth of a new nation. The early years were marked by a series of challenges, including the Revolutionary War and the struggle to establish a stable government. The Constitution was drafted in 1787, providing a framework for the new republic. The period from 1789 to 1861 saw the United States expand its territory, develop its economy, and face internal conflicts. The War of 1812, the Missouri Compromise, and the Nullification Crisis were key events that shaped the nation's identity. The era ended with the outbreak of the Civil War in 1861, which would ultimately lead to the abolition of slavery and the preservation of the Union.

The early years of the United States were marked by a series of challenges. The Revolutionary War, which began in 1775, was a struggle for independence from British rule. The war ended in 1781 with the signing of the Treaty of Paris, which recognized the United States as a sovereign nation. The new nation faced the task of establishing a stable government. The Articles of Confederation, the first constitution, proved to be inadequate, leading to the drafting of the current Constitution in 1787. The Constitution established a federal government with three branches: the executive, the legislative, and the judicial. The first President, George Washington, was inaugurated in 1789. His administration was marked by the Whiskey Rebellion and the Jay Treaty, which helped to resolve tensions with Britain.

The period from 1789 to 1861 saw the United States expand its territory. The Louisiana Purchase of 1803 doubled the size of the nation. The acquisition of Florida in 1819 and the Texas Annexation in 1845 further expanded the country's borders. The expansion of territory led to the development of a new economy. The invention of the cotton gin in 1793 revolutionized the cotton industry, leading to a boom in cotton production. The growth of the cotton industry was closely tied to the institution of slavery, which provided the labor for the plantations. The period also saw the rise of the industrial revolution in the Northeast, which transformed the economy and society. The invention of the steam engine and the development of factories led to a rapid increase in production and a shift from an agrarian to an industrial society.

The era from 1789 to 1861 was marked by a series of internal conflicts. The War of 1812, fought between the United States and Britain, was a significant event that tested the nation's military and political strength. The war ended in a stalemate, but it helped to establish the United States as a major power. The Missouri Compromise of 1820 was a landmark decision that resolved a dispute over the admission of new states. The Nullification Crisis of 1832-33 was a constitutional crisis that threatened the unity of the nation. The crisis was resolved by the Compromise Tariff of 1833, but it highlighted the tensions between states' rights and federal authority. The era ended with the outbreak of the Civil War in 1861, which was a result of the long-standing conflict over slavery. The war would ultimately lead to the abolition of slavery and the preservation of the Union.



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## PRELIMINARY REPORT ON FIRE HAZARD RATING STUDY

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(Supplement to 1932 Annual Fire Weather Report,  
California District)

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INTRODUCTIONNeed for fire hazard rating

Definite and quantitative rating of fire hazard may be said to be the ultimate aim and central problem of fire control and fire weather researches. In view of present knowledge, scientifically precise rating is but a remote future possibility, due to the great number of complex and variable factors involved. Practical approximations, more or less rough, are all that can be expected at present. Both the forester and the meteorologist increasingly find that definite rating is essential to the most effective fire control and to the forecasting and study of fire weather. To the meteorologist, definite rating will permit of forecasts having more definite meaning in terms of expected fire hazard, and will furnish a suitable scale for comparison in studies of fire weather. To the forester, such rating will mean a more definite knowledge of past, current and prospective fire hazard, which in turn will promote more effective fire control in terms of any accepted economic standard of forest protection.

Requirements of scale

It is essential, of course, that any rating scheme finally adopted must agree with observed facts, and yet deal practically with the broader rather than the greatly detailed aspects of the problem. It is desirable that formulae be developed expressing all important relationships, but tables and graphs in simplest form are better adapted for field use, and should be employed since they reduce the labor and skill required for calculation and tend to minimize error. The units used in





the scale must be those most easily calculated and measured, and must be of such nature as to permit ultimate correlation with the primary factors involved in measurement of fire control effort and results, such as man power, funds, equipment and damage. The factors considered in such a rating scheme should be only those of fundamental or real importance in the broad view of the problem. Greatly detailed mathematical analysis is beyond present possibility or would lead to relationships too intricate for practical use.

### Methods of attack on rating problem

There are essentially three methods of attack on the fire hazard rating problem, although obviously all must be employed, either directly or as checks, in securing final rating relationships.

1.) THEORETICAL METHOD-general physical law applied mathematically and otherwise, supplemented by hypotheses where current theory is lacking or obviously inadequate.

2.) EXPERIMENTAL METHOD- laboratory or field experimentation to determine facts, supplement theory and verify hypotheses.

3.) EMPIRICAL METHOD-crudely, the application of judgement gained by practical experience; more definitely, solution by means of detailed statistical analysis of records representing field experience.

### Scope of this report

In view of the complexity of the problem, this report must be considered merely as suggestive of possible modes of attack and of the principal factors which apparently must be considered in any satisfactory rating scheme. The report indicates the progress made, using the theoretical method. Much of the literature of combustion and related subjects is obscure and faulty, and a wide variation in values of physical constants used appears. This report, therefore, attempts to collect and consolidate for ready use some of the widely scattered material directly pertinent to fire hazard rating study, and to indicate suitable values for the various constants. The data given have been checked by search through many





references and represent, so far as known, the best values available for practical fire hazard rating work. In some cases it has been necessary to attempt to reconcile differences and adopt compromise values, and in other cases, where authorities differed, the value favored by the apparently "best" authority has been used.

This report is limited to discussion of forest fire hazard as distinct from other types of fire hazard. It is a progress report, of preliminary nature, and if some of the broad scale relationships are more definitely indicated than heretofore, its purpose will have been accomplished.

#### PRINCIPAL GENERAL FACTORS AFFECTING FIRE HAZARD RATING

##### Fire hazard defined

The term "fire hazard", used in a general sense, may be defined as the danger, risk, chance or probability of fire.

##### The two aspects of general fire hazard

Fire hazard in general, as defined above, must be considered from two aspects.

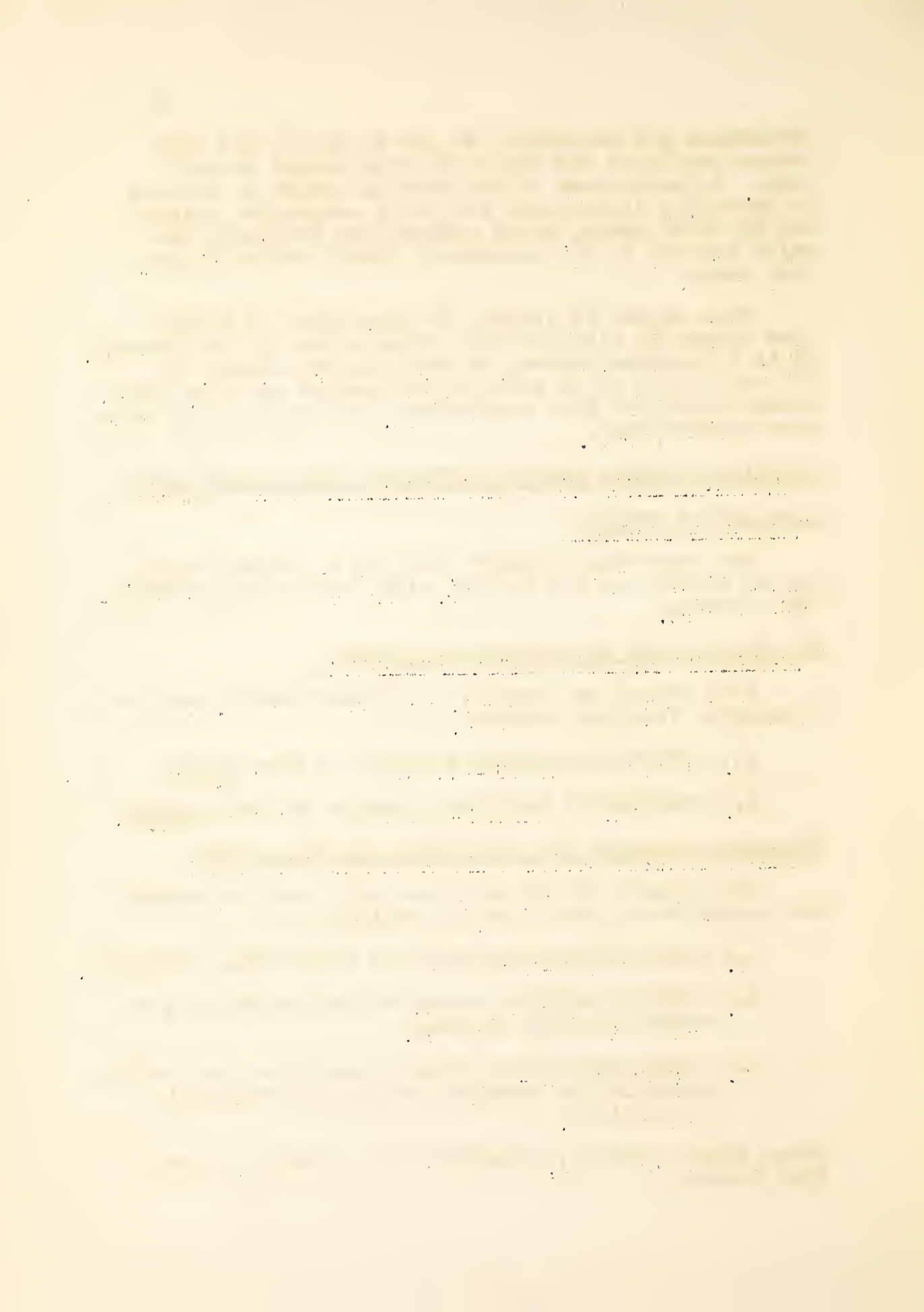
- 1.) INCEPTION HAZARD-the danger of fire start.
- 2.) TRANSLATION HAZARD-the danger of fire spread.

##### Elements necessary for combustion and fire hazard

The elements which simultaneously must be present and operative so that fire is possible are

- 1.) FUEL SUPPLY-inflammable or combustibile material.
- 2.) IGNITING AGENT-a source of heat sufficient to cause ignition of fuel.
- 3.) OXYGEN SUPPLY-the element permitting and making possible the chemical reactions involved in combustion.

These three elements, together with a fourth, control fire hazard.



- 4.) MODIFYING INFLUENCES-numerous factors affecting the foregoing three elements, especially in a quantitative sense.

### PRINCIPAL DETAILED FACTORS AFFECTING FIRE HAZARD RATING

The following brief outline indicates in greater detail those factors which must be considered in any really satisfactory rating scheme. The outline may not be complete, but it does indicate the principal and obvious factors involved in fire hazard.

#### 1. FUEL SUPPLY

- a. Species (general, as coniferous, deciduous, hardwood, softwood; specific, as western yellow pine, California live oak, etc.).
- b. Type (light, as duff, grasses, ferns, mosses; heavy, as whole trees, snags, logs, stumps, etc.).
- c. Mensuration factors (quantity, size, shape, ratio of surface to mass and volume).
- d. Moisture factors (living or dead, fuel moisture content, state of moisture (solid, liquid, vapor)).
- e. Heat factors (heating value, specific heat, actual fuel temperature, ignition temperature).
- f. Disposition (detached, above ground, as tree crowns; compact ground layer, as duff; etc.).
- g. Physical structure and behavior.
- h. Chemical structure and behavior.

#### 2. IGNITING AGENT

- a. Nature (type, size, shape, ratio of surface to mass and volume, disposition, physical structure and behavior, chemical structure and behavior).
- b. Moisture factors (moisture content, state of moisture).
- c. Heat factors (actual temperature, heating value, life, duration and rate of heat output, manner of application, atmospheric and other influences on effective heat).
- d. General factors (transport of sparks and embers, convection, conduction and radiation of heat).

#### 3. OXYGEN SUPPLY

- a. Nature (from air and fuel).
- b. Amount (as affected by meteorological and physical conditions, including products of combustion and degree of effective contact with fuel).



#### 4. MODIFYING INFLUENCES

- a. General (topographic, as slope shape, aspect and steepness; altitude, geographical location).
- b. Atmospheric factors (temperature, humidity, pressure, wind force and movement, cloudiness, precipitation, solar radiation, evaporation).
- c. Soil factors (nature of soil, temperature, moisture content and height of water table, evaporation losses of moisture, specific heat).
- d. Fire factors (size, shape, perimeter, amount of heat generated).
- e. Abstract factors (units used for measurement and calculation, standard conditions as reference points; type of mathematical formulation employed, etc.).

### DISCUSSION

#### General theory of combustion

Combustion or burning may be defined as a chemical union of constituents of a fuel with oxygen, accompanied by the evolution of heat. Usually the term "combustion" is applied to the reaction when it is violent and rapid. The term "oxidation" is used, rather loosely, when the reaction is mild and slow, relatively. In a sense, then, combustion is merely rapid oxidation and oxidation is merely slow combustion. The rate of the reaction largely determines whether the phenomenon is combustion or oxidation, as well as the amount of heat evolved in unit time. The burning of wood, oil or coal is ordinarily rapid and is representative of a combustion process. The rusting of iron, the decay of wood, and the utilization of food substances by the human body are types of oxidations, in which the reactions are slower than in active combustion, but result in the same products as in ordinary combustion. The liberation of heat by rusting iron or decaying wood is slow, and is not readily perceptible. By the physical principle of the conservation of heat (or energy), however, the same total amount of heat is liberated regardless of the speed of the reaction, whether combustion or oxidation. If the reaction is slow, the evolved heat is carried away by conduction, convection and radiation as fast as liberated. If the reaction is rapid, heat may be evolved faster than these processes can carry





it away, and hence the temperature rises appreciably. If the material (such as hay or rags) is a poor heat conductor, and there is sufficient air for oxidation but not enough to remove the heat generated, heat may accumulate and cause a temperature sufficiently high to initiate active combustion. Such action is termed "spontaneous" combustion.

### Products of combustion

The products of combustion (or oxidation) are chemical substances resulting from the union of fuel constituents with the oxygen of the air, plus heat. For wood fuels (which contain practically no sulphur), the products of complete combustion are H<sub>2</sub>O (water vapor), CO<sub>2</sub> (carbon dioxide gas) and N<sub>2</sub> (nitrogen gas). If combustion is incomplete by reason of insufficient oxygen to combine with all of the carbon of the fuel, the products are H<sub>2</sub>O, N<sub>2</sub> and CO (carbon monoxide gas), the latter instead of or in addition to a smaller amount of CO<sub>2</sub>. Quantitatively, the products of combustion are as follows:

TABLE 1  
Products of Combustion

Combustible Chemical Elements	Ant. Oxygen (lbs.) re- quired for each lb. of combustible	Products*	Lbs. products per lb. of combustible
H (Hydrogen)	7.94	a:H <sub>2</sub> O & 51658 Btu <sub>77°</sub> heat b:H <sub>2</sub> O & 6505 Btu <sub>77°</sub> heat c:H <sub>2</sub> O & 5778 Btu <sub>77°</sub> heat d:H <sub>2</sub> O & 61093 Btu <sub>77°</sub> heat e:H <sub>2</sub> O & 7694 Btu <sub>77°</sub> heat f:H <sub>2</sub> O & 6833 Btu <sub>77°</sub> heat	6.94
C (Carbon) (Complete Combustion)	2.67	a:CO <sub>2</sub> & 14352 Btu <sub>77°</sub> heat b:CO <sub>2</sub> & 5309 Btu <sub>77°</sub> heat c:CO <sub>2</sub> & 3861 Btu <sub>77°</sub> heat	3.67
C (Carbon) (Incomplete Combustion)	1.33	a:CO & 5963 Btu <sub>77°</sub> heat b:CO & 2973 Btu <sub>77°</sub> heat c:CO & 1699 Btu <sub>77°</sub> heat	2.33

See next page for references.





References, Table 1:

\*Quantities of heat developed in reaction indicated differently, as follows:

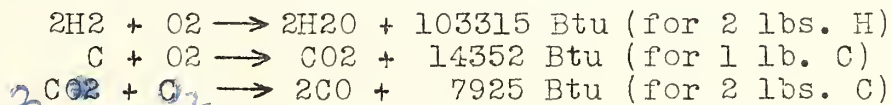
- a: Gaseous product; heat per lb. of combustible.
- b: Gaseous product; heat per lb. of oxygen.
- c: Gaseous product; heat per lb. of product.
- d: Liquid product; heat per lb. of combustible.
- e: Liquid product; heat per lb. of oxygen.
- f: Liquid product; heat per lb. of product.

#Btu: British thermal unit; the amount of heat required to raise the temperature of one pound of pure water through one degree Fahrenheit, defined at 60 F.

The values given in table 1 were converted to English units from data given in the International Critical Tables (1). These heats of formation are for 64.4 F.

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The chemical equations representing the reactions involved are as follows:



Nitrogen in fuels is considered to be evolved as a gas uncombined with any other chemical element during the process of combustion, and without the evolution of any heat. The incombustible mineral constituents of the fuel are unaffected and remain behind as a solid residue (ash).

The atomic weights used for calculation of Table 1 data are as follows:

O (oxygen).....	16.0000
H (hydrogen).....	1.0077
C (carbon).....	12.0050

The process of combustion or oxidation is an extremely interesting example of energy transformation. Thus, plants take CO<sub>2</sub> from the air, H<sub>2</sub>O from the soil, and N<sub>2</sub> from the soil and by means of solar energy (heat) manufacture plant substances of complex CHNO (carbon, hydrogen, nitrogen and oxygen) composition. Combustion reverses this process by evolving CO<sub>2</sub>, H<sub>2</sub>O, N<sub>2</sub> and heat from plant substances.



## Fuel composition

The fuels involved in forest, brush, grass and grain fires are the various woods and woody substances, or fibers consisting principally of cellulose ( $C_6H_{10}O_5$ )x. Wood may be said, in general, to consist of cellulose plus a number of complex infiltrating substances collectively termed "lignin". It has been found that the general chemical composition of woods of various species is approximately the same, averages for woods common to the United States being as follows:

TABLE 2  
Average Chemical Composition of Dry Wood (2)

<u>Element</u>	<u>% by weight</u>
Carbon (C).....	49.70
Hydrogen (H).....	6.06
Oxygen (O).....	41.30
Nitrogen (N).....	1.05
Ash (incombustible mineral matter, composition not specified).....	1.89
	<u>100.00</u>

The foregoing table is only approximately correct, because the content of resinous materials (saps, gums, resins, oils, etc.) of various woods differs in the relative proportions of each of many complex carbon compounds. The table, however, agrees closely with the composition of various woods, when reduced to chemical elements, without considering in what compounds these elements occur.

## Density of wood substance

Since the composition of various woods is much the same, at least for the practical purpose of rating fire hazard, it follows that the density or specific gravity of wood substance itself, as well as its specific heat and heating value, should also be much the same for different species. Determinations made at the Forest Products Laboratory of the Forest Service at Madison, Wisc., on seven species of wood including both hardwoods and conifers, showed a range of only about  $4\frac{1}{2}\%$  in the density of wood substance, or material of which the cell walls are composed. Since the density is so nearly constant, it may be said that



the density of a given piece of dry wood (including wood substance and vacant cell spaces) is a measure of the amount of actual wood substance contained in it (3). Hawley and Wise (4) quote values for the density of wood substance (determinations made by Dunlap) ranging from 1.50 to 1.57, but state that these results probably are too high, and that the value of 1.475 (by Stamm) is nearer the truth, but still slightly too high. A value of 1.47 is adopted for this report.

### Density of wood

The density of wood, as distinct from wood substance, refers to the weight of the wood sample oven dry divided by the weight of an equivalent volume of water. If the oven dry weight and the oven dry volume are used in determining the density, the oven dry density results. Green and air dry densities may also be used. However, for fire hazard rating purposes, it is preferable to use oven dry densities determined from the relation

$$\frac{\text{wt. wood oven dry}}{\text{wt. H}_2\text{O in oven dry volume}}$$

rather than the air dry or green densities, since the shrinkage and swelling wood undergoes with changes in moisture content would complicate calculations unnecessarily. The following table gives values for oven dry densities, taken from the International Critical Tables (1), to which reference should be made for woods not listed.

TABLE 3

### Oven Dry Densities of Common Woods

<u>Wood</u>	<u>Origin</u>	<u>Density</u>
ALDER, red.....	Wash.....	0.434
ASH, Oregon.....	Ore.....	0.575
CASCARA.....	Ore.....	0.548
CEDAR, Alaska.....	Ore.....	0.439
CEDAR, incense.....	Ore.-Cal.....	0.365
CEDAR, Port Orford..	Ore.....	0.440
CEDAR, western red..	Mont.-Wash.....	0.344
CHINQUAPIN, golden..	Ore.....	0.483
COTTONWOOD, black...	Wash.....	0.368
DOGWOOD, Pacific....	Ore.....	0.701

(continued on next page)



TABLE 3 (continued)

<u>Wood</u>	<u>Origin</u>	<u>Density</u>
ELDERBERRY, blue.....	Ore.....	0.570
FIR, Douglas; coast.....	Wash.-Ore.-Cal.....	0.512
FIR, Douglas, mountain.....	Wyo.-Mont.....	0.446
FIR, lowland white.....	Mont.-Ore.....	0.419
FIR, Noble.....	Ore.....	0.403
FIR, red.....	Cal.....	0.421
FIR, silver.....	Wash.....	0.415
FIR, white.....	Cal.-N.Mex.....	0.397
GUM, blue.....	Cal.....	0.796
HEMLOCK, mountain.....	Mont.....	0.480
HEMLOCK, western.....	Wash.-Ore.....	0.432
JUNIPER, alligator.....	Ariz.....	0.545
LARCH, western.....	Mont.-Wash.....	0.587
MADRONA.....	Ore.-Cal.....	0.694
MAPLE, bigleaf.....	Wash.....	0.513
MYRTLE, Oregon.....	Ore.....	0.589
OAK, California black...Ore.-Cal.....		0.578
OAK, Canyon live.....	Cal.....	0.838
OAK, Gambel.....	Ariz.....	0.701
OAK, Oregon white.....	Ore.....	0.748
PINE, Jeffrey.....	Cal.....	0.425
PINE, lodgepole.....	Wyo.-Mont.-Colo.....	0.434
PINE, sugar.....	Cal.....	0.378
PINE, western white.....	Mont.-Idaho.....	0.418
PINE, western yellow..Wash.-Cal.-Colo.-Mont.-..		0.420
PINON.....	Ariz.....	0.567
REDWOOD, gigantea.....	Cal.....	0.290
REDWOOD, sempervirens...Cal.....		0.436
SPRUCE, Sitka.....	Wash.-Ore.....	0.397
WILLOW, western black...Ore.....		0.473
YEW, Pacific.....	Wash.....	0.673

The need for data relating to wood densities in fire hazard rating will be apparent later. For the most accurate rating, it would be desirable to have density determinations at intervals, since the values given above are merely averages, and woods of the same species in groves only a short distance apart might easily have materially different densities. It also will eventually be necessary to have values for the foliage of various species, for grasses, ferns, tree mosses, bark and other light fuels.

#### Heating value of woods

While the composition of wood substance is fairly constant for practically all species, there is con-



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siderable variation in the amount of resinous material present in the cell spaces, as also in the nature of the resinous material. The approximate specific gravity of the resinous material is roughly 0.88, and its heating value per pound is about 17400 Btu according to Hawley and Wise (4). It is possible to calculate approximately the heating value of various fuels from the percentage composition, by Dulong's formula, but the best results are those obtained by careful calorimeter measurements, since the resinous materials cannot be entirely satisfactorily evaluated by formula. Dulong's formula appears in several forms in different "standard" textbooks on combustion, a common form being

$$HV = 14500 C\% + 62100 \left( H\% - \frac{O\%}{8} \right)$$

where HV is heating value per pound of fuel in Btu, C is percentage of carbon by weight in one pound of fuel, H and O are similar percentages of hydrogen and oxygen. This formula assumes that the oxygen already in the fuel is, in effect, already combined with a suitable amount of the hydrogen, and hence takes no active part in the combustion so far as effective heating is concerned. The values of heat for complete combustion of carbon (14500) and hydrogen (62100) differ rather materially from values given by the International Critical Tables (1) already cited in Table 1. Further, the value for hydrogen assumes that the H<sub>2</sub>O produced by combustion is in liquid form, which cannot be the case, in view of the temperatures necessary for combustion. The basic form of this formulae will be employed later in connection with oxygen supply, but will not be used for computations of heating value. The literature of fuels gives widely varying values for the heats liberated by complete combustion for different woods. Hawley and Wise (4) consider Parr's results best, and they will be adopted tentatively for this report. The following table gives Parr's averages, corrected to a dry fuel basis by Hawley:

TABLE 4  
Heating Value of Dry Woods\*

Pine.....8836	Oak.....8556	Hickory....8448
Cherry....8623	Birch.....8458	Poplar.....8640
Following estimated from data in (2)		
Fir.....8749	Ash.....8725	Elm.....8755

\* In Btu per lb. of dry fuel.

Average of 6 Parr values....8534



CHEMICAL COMPOSITION AND HEATING VALUE OF  
COMMON DRY WOODS

Wood	Chemical Elements <sup>#</sup>				Ash	Heating Value*
	C	H	N	O		
OAK	50.13	6.02	0.09	43.36	0.37	8316
ASH	49.18	6.27	0.07	43.91	0.57	8480
ELM	48.99	6.20	0.06	44.25	0.50	8510
BEECH	49.06	6.11	0.09	44.17	0.57	8591
BIRCH	48.88	6.06	0.10	44.67	0.29	8586
FIR	50.36	5.92	0.05	43.39	0.28	9063
PINE	50.31	6.20	0.04	43.08	0.37	9153

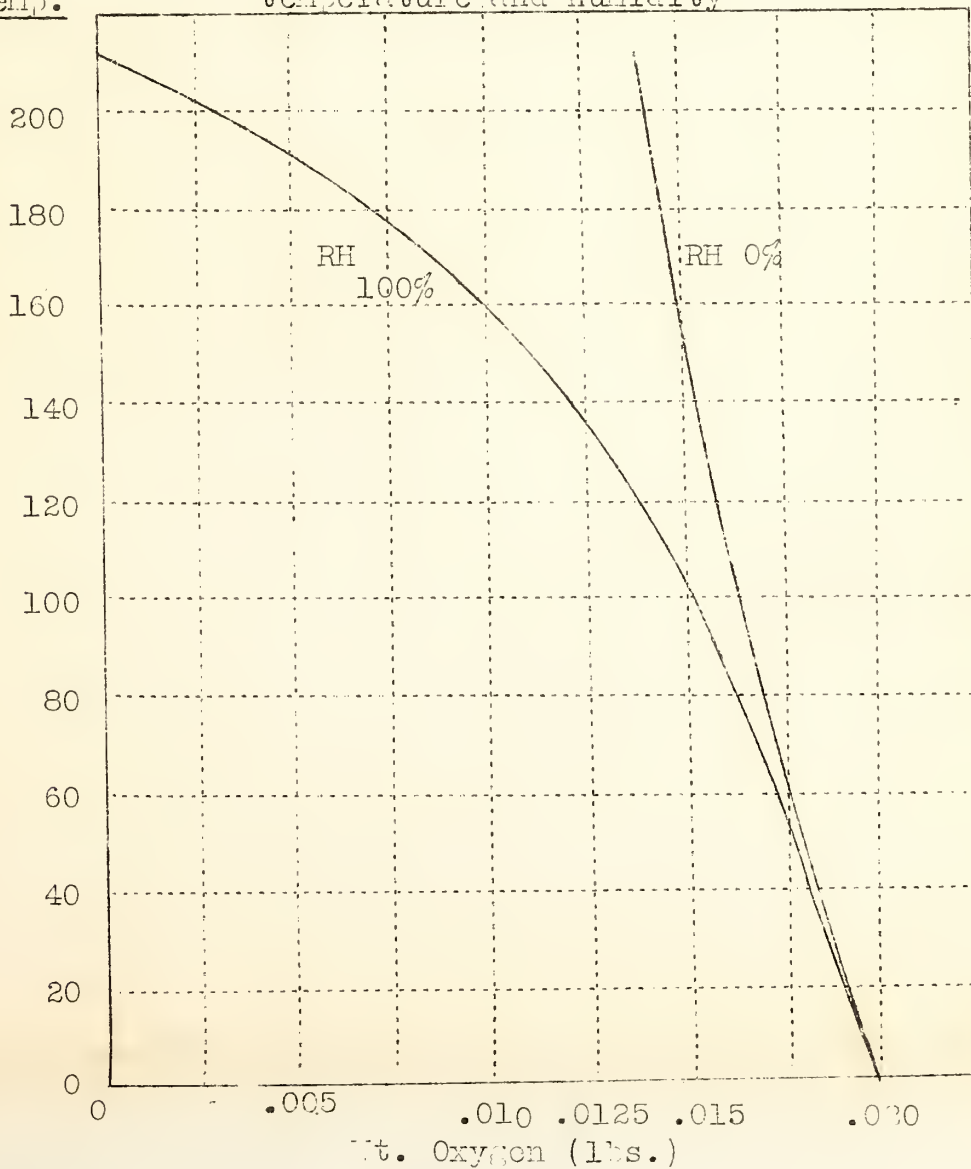
# in % by weight per lb. of dry wood; C: Carbon; H: hydrogen; N: Nitrogen; O: Oxygen.

\* In Btu per lb. of fuel (wood).

Modified from "Elements of Steam and Gas Power Engineering", by Potter and Calderwood, p. 30 (values from determinations by Poole).

FIGURE 5

Weight of Oxygen per cubic foot of air as affected by  
Temp. temperature and humidity





These values are unsatisfactory in the sense that many species of pine, for example, with differing resinous material contents, are lumped under one designation. Satisfactory values for grasses, ferns, tree mosses, etc. also must be secured before values adequate for fire hazard rating computations may be said to be available. There is also the factor of possible variation in heating values for woods of the same species but of different ages, different physiological condition and from different, though possibly adjoining, areas. However, the foregoing values will be used tentatively, as illustrating the method of computation to be developed later in this report.

### Ignition temperatures

Engineering practice assumes certain fixed ignition or kindling point temperatures for each fuel, that is, temperatures at which active combustion rather than slow oxidation starts. Temperature is not the only factor concerned, however. Finely powdered iron will start burning at a lower temperature than will iron wire, because it presents relatively more surface to the oxygen of the air in proportion to the quantity of material present. This factor of ratio of surface to volume and mass is operative in forest fires. Thus, the finer and lighter fuels (grasses, twigs, needles, etc.) ignite more readily than the coarser and heavier fuels (stumps, logs, snags, etc.), even though the chemical composition is practically identical. The smaller the quantity of oxygen present (as affected by air pressure, for example), the more difficult ignition becomes. The vapor of methyl alcohol in air must be raised above a red heat before combustion starts, but the same mixture in pocket lighters ignites readily by means of a thin platinum wire acting as a contact or catalytic agent without any other source of heat. Thus, strictly, no definite kindling temperature can be given unless the other conditions are specified, such as the nature and condition of the fuel, the amount of oxygen available, the ratio of surface to volume and mass, the presence or absence of a contact agent, and its nature.

Wood fuels, upon being heated, evolve volatile products which ignite at lower temperatures than does the fixed carbon (charcoal) of the wood substance.





Hence, any fixed ignition temperature assumed for purposes of calculation is really equivalent to an approximate average temperature at which the most ignitable components of a fuel will begin to burn under favorable, if not optimum, conditions.

Hawley and Wise (4) state that the burning of wood involves two general aspects,

- 1.) The conditions under which wood will ignite and burn, and
- 2.) Its heat of combustion.

According to these authors, ignition depends on the method and rapidity of heating, the air supply and so far as statement of an actual temperature is concerned, on the place where the temperature of ignition is measured, among other factors. They state that all woods begin to decompose (give off volatile products) at a temperature of about 275 C. or 527 F.; provided the wood is dry. Exceptions occur, however, due to

1. ) The physical properties of the wood concerned, such as porosity in its influence on the surface of contact between the wood and air, and

- 2.) The presence of extractives with low ignition temperatures, such as volatile oils.

They state further that combustion once started continues so long as air supply and heat of combustion are not materially affected, the latter in the sense that the heat evolved is not dissipated, but heats new portions of fuel to the ignition temperature. Chemically; the combustion of wood may be divided into two stages,

- 1.) Combustion of vapors and gases given off by the exothermal (heat liberating) decomposition of wood.

- 2.) The combustion of the solid residue of charcoal left behind after the exothermic reaction is completed.

The charcoal appears to act as a catalytic agent in wood combustion. It is important to bear in mind that the outside of a stick can burn at 275 C. without heating the interior above this point, due to radiation and conduction losses to the air.





Kochler (5) describes the ignition and combustion of wood substantially as follows: At 212 F. slight and gradual decomposition begins. At 320 F. decomposition is more rapid and the wood has a charred appearance. At 480 F. the wood has the appearance of brownish charcoal, and at 575 F. and higher the charcoal is black and metallic. At 400 C. or 752 F. all woods ignite very quickly, but the lighter woods burn more readily. "Wood" ignites spontaneously at temperatures slightly over 525 F., and sound hemlock has been ignited at 428 F. and decayed hemlock at 406 F. without a pilot flame to ignite the evolved gases.

Various other references, principally engineering handbooks, give ignition temperatures as follows:

Dry Charcoal.....	660 deg. F.
Dry Pine Wood.....	800 deg. F.
Dry Oak Wood.....	900 deg. F.

It is probable that these values are rough averages based upon air dry wood, which may contain 12% or more moisture, or that special conditions of oxygen supply and other factors were involved. In any case, they seem too high in view of the foregoing, and hence will be disregarded. Hawley (6) and Gisborne (7) have taken 540 F. as the approximate ignition temperature for the average dry fuels concerned in forest fires, and this value will be adopted in this report, for use as a reference point in computations.

#### Species factors and related miscellaneous factors

Average values for density, volume of fuel per unit area, surface area of that volume, ignition point and heating value must be secured or approximated in order for proper evaluation of these factors in fire hazard rating formulae. Such values may most suitably be presented in tabular or graphical form. Quantity and type of fuel may be approximated, apparently, for California at least, from data collected in connection with the cover type map.

Practically the only fuel shapes which must be considered are the cylindrical (twigs, branches, trunks) and flat (deciduous leaves, duff layer, etc.).



## Moisture factors

The moisture content of fuels acts to

- 1.) Prevent contact of oxygen with wood substance.
- 2.) Increase the amount of heat required for ignition and combustion.

In the first case, contact is prevented, at least partially, so long as the wood contains any water whatever. After being driven off from the wood by heat, the water vapor will add to the amount of water vapor available to displace air and reduce the effective amount of oxygen in that way. In the second case, water in the fuel must be raised to the boiling point, must be vaporized, and the vapor raised to the ignition point, prior to ignition, assuming that water must be entirely removed from any given limited surface before combustion can occur. It appears from experiments by Dunlap, quoted by Koehler (5), that some heat is required to entirely remove the hygroscopic water remaining after ordinary evaporation, ranging from 29.7 Btu for sugar maple to 35.3 Btu for longleaf yellow pine. This heat is necessary to overcome the chemical attraction of the wood substance for the water. According to the International Critical Tables (1), this heat of complete wetting, in Btu per pound of dry fuel (as for the Dunlap values), is 14.6 Btu for powdered cellulose dried in vacuo at 250.8 F. and 28.8 Btu for powdered wood fiber (species not given). Provisionally, this heat of wetting will be taken at 30 Btu per pound of dry material for deciduous species and 35 Btu for the resinous conifers. The wood itself must be raised to the ignition temperature, and this quantity of heat is additive to all of the foregoing.

Hawley (6), using two one pound blocks of wood, identical except for moisture content, calculated the number of Btu required to raise the fuel samples to an ignition temperature of 540 F. from an air temperature of 50 F., under standard atmospheric pressure (29.921") and boiling point of 212 F., as follows:

Block A (20% moisture)		Block B (5% moisture)
Btu	<u>Operation</u>	Btu
160.00	Raising wood to 540 deg. F.	160.00
32.40	Raising water to 212 deg. F.	8.10
193.00	Vaporizing water	48.25
<u>32.80</u>	Raising vapor to 540 deg. F.	<u>8.20</u>
418.20	TOTALS	224.55
258.20	Totals, excluding wood	64.55



From this calculation it is seen that the heats relating to the water in the fuel are proportional to the fuel moisture contents expressed as percentages, thus:

$$\frac{64.55}{258.20} = \frac{5}{20} = \frac{1}{4}$$

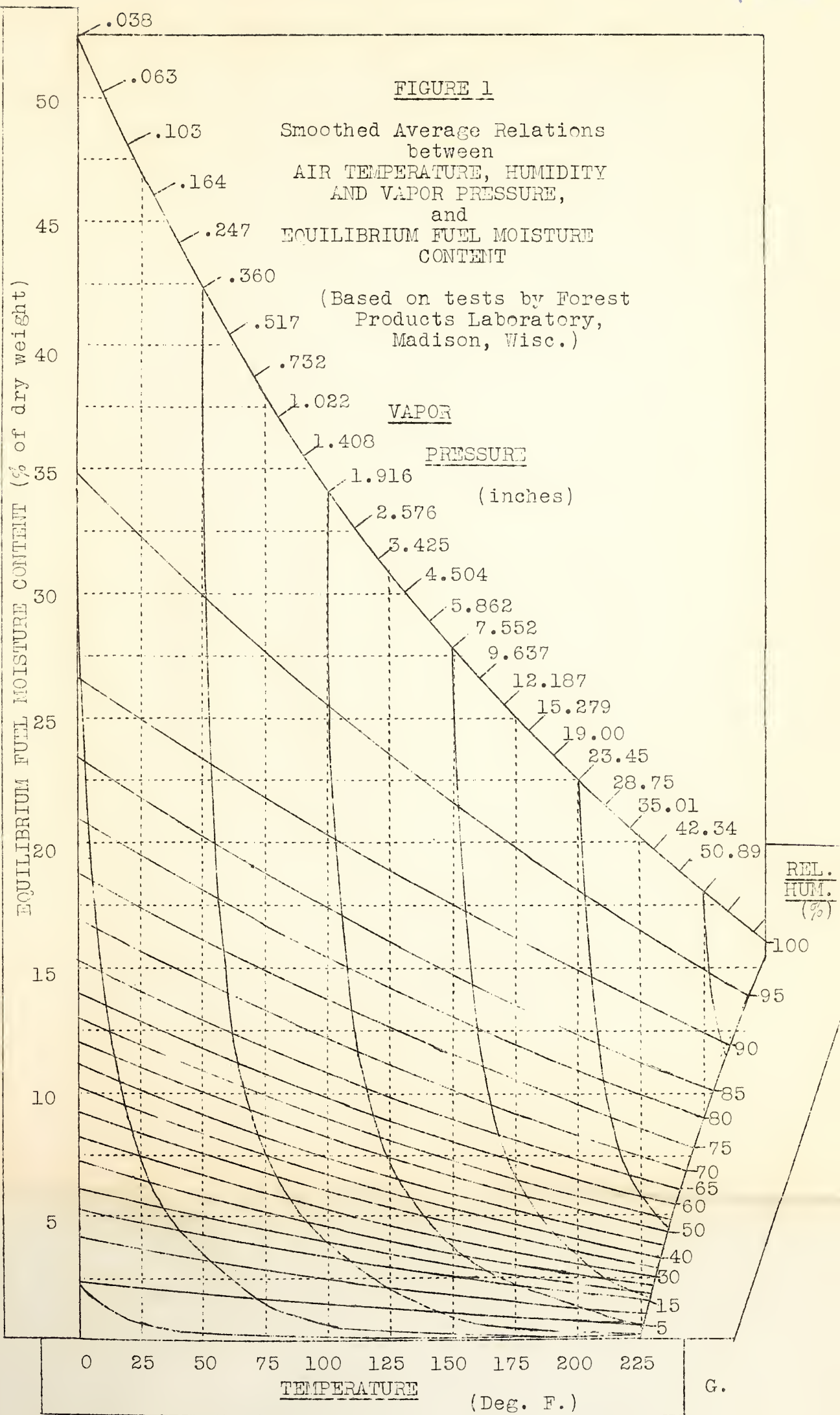
While other factors apparently must be considered in determining the amount of heat necessary for ignition, as will appear later, this calculation shows that four times as much heat is required to eliminate the water from Block A compared with Block B, and that, so far as moisture is concerned, inception hazard is inversely proportional to fuel moisture content.

### Fuel moisture content

The moisture in fuels may be absorbed from the air, the soil or through precipitation and condensation processes, such as rain, snow, dew or frost. Wood is a complex arrangement of cells, with void spaces or cell openings in addition to the wood substance in the cell walls. The cell walls themselves are capable of holding moisture; this moisture is termed "fiber" moisture, or hygroscopic moisture. When the cell walls hold their maximum capacity of moisture at any given temperature, the "fiber saturation point" is said to have been reached, and no further changes in volume (swelling) will take place when additional moisture is taken up by the cell spaces or voids. Any drop in cell wall moisture content below the fiber saturation point causes shrinkage of the wood sample. The moisture taken up by void spaces is termed "free" water. The moisture in cell walls is absorbed from the air; moisture in free form in the voids does not occur unless the fuel is immersed in water or is directly wetted by precipitation. When both the cell walls and the voids are holding their moisture capacity, the wood is said to be completely saturated. All species tested have been found to have approximately the same equilibrium fuel moisture values, by equilibrium being meant the condition when the wood neither gains nor losses moisture under any existing conditions of temperature and relative humidity of the air from which absorption occurs. Gisborne (7) says: "results of laboratory tests (at Forest Products Laboratory, Madison, Wisc.) were so nearly alike for the materials tested that for all practical purposes the different materials may be said to have the same equilibrium moisture content for any particular temperature and relative humidity".











Wood is a colloid, that is, a chemical compound of such nature that it forms a colloidal suspension or solution with water, the wood substance becoming partially converted to a gel in the process, with consequent reduction in strength and increased pliability. The absorption of water by wood, as with other hygroscopic materials, is a complex process. It is probable that there is a chemical solution of water in wood, and that capillarity, surface tension and adsorption are factors involved. There are two explanations for the fact that water is condensed to liquid form in the wood, from the air, without high humidity or appropriate temperature changes. One is that the condensation occurs as the result of very fine capillaries in the wood affecting vapor pressure to such an extent as to cause condensation, and the other is that both wood particles and atmospheric water vapor are electrically charged and the water vapor is attracted and condensed by wood particles of opposite charge. This is the present partial explanation for the phenomenon of adsorption. Moisture thus adsorbed on the wood surface is absorbed by the wood through capillary and surface tension phenomena.

Peck (3) describes the phenomena as follows: "Wood substance, mainly cellulose and lignin, is a hygroscopic material, i.e.-it possesses the power to remove water vapor from the surrounding atmosphere. The water removed is caused to go into solution with wood, forming what might be called a solid solution. In any atmosphere of constant conditions, the process of absorption of water by a piece of wood continues until the vapor pressure of the solution is equal to that of the atmosphere. The wood will have then attained what is called an equilibrium fuel moisture content. If the temperature of the atmosphere and wood were raised, water would pass from the wood to the atmosphere, but if the temperature were lowered, the reverse would take place. This means that for a given vapor pressure of the solution, the lower the temperature the greater will be the concentration, or the more water the wood can dissolve."

In general, the properties of colloidal solutions as to boiling and freezing points are not affected as in other solutions, and advantage of this property can be taken in fire weather and fire hazard computations as will appear later.



The relations between equilibrium fuel moisture content, and air temperature, relative humidity and vapor pressure are shown in Figure 1, adapted from a diagram in (8). The vapor pressure lines are merely guide lines. A diagram of this nature is very useful in estimating the effects of given changes in temperature and humidity on fuel moisture. While the approach to equilibrium conditions is very slow for heavy fuels, the lighter fuels (such as the surface layer of duff, grasses, ferns, mosses, etc.) respond rather rapidly to atmospheric changes, with lags varying from about one hour for fireweed to 3 or 4 hours for the heavier types of duff. It should be borne in mind, in the absence of detailed data showing the rate of attainment of equilibrium fuel moisture conditions by various fuels, that the graph merely indicates the trend of the change that will occur, and if the conditions remain constant for a relatively long time, the values of fuel moisture that ultimately will be reached under the given conditions.

For example, assuming a fuel moisture of 20%, relative humidity 85%, temperature 55 F., a point will be found on the graph lying on the vapor pressure line for .360". If the temperature is raised to 75 F., with vapor pressure constant (no importation or exportation of moisture), the new equilibrium value towards which the fuel moisture will tend is found by tracing down the vapor pressure line .360" to its intersection with 75 F., which point shows a fuel moisture of 7.5%. With these same conditions, lowering the temperature to 50 F. would result in a fuel moisture of 42.5%. The graph shows the equilibrium fuel moisture at any temperature and humidity (within its range), and the changes produced by varying temperature or humidity, or both. Table 5 shows actual values obtained from various sources and smoothed to a degree apparently justified by theoretical considerations.

The experimental values on which Table 5 and Figure 1 are based are faulty in the sense that the duration of the tests was not sufficient to insure that equilibrium values were reached for the higher humidities. Why this is so will be evident from the facts that a good sized white pine log, perfectly dry, would have to be immersed in water for more than five years to soak up its capacity of water (9) and that Douglas fir sticks 4"x8"x6' were not fully saturated after seven years submersion (5). McKenzie (4) found



TABLE 5

EQUILIBRIUM FULL MOISTURE CONTENT\*  
IN RELATION TO  
AIR TEMPERATURE AND RELATIVE HUMIDITY

Rel. Hum. %	(for wood) Temperature (deg. F.)							
	0	32	50	75	100	125	150	212
0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
5	2.4	2.0	1.8	1.6	1.4	1.2	1.0	0.7
10	4.2	3.6	3.4	3.0	2.7	2.4	2.0	1.4
15	5.3	4.5	4.2	3.8	3.4	3.0	2.6	1.8
20	6.3	5.4	5.0	4.5	4.0	3.5	3.1	2.2
25	7.4	6.3	5.8	5.2	4.6	4.1	3.6	2.6
30	8.3	7.2	6.6	5.9	5.3	4.6	4.1	2.9
35	9.2	8.1	7.5	6.7	6.1	5.3	4.7	3.4
40	10.2	9.0	8.4	7.5	6.8	6.0	5.3	3.8
45	11.1	9.8	9.2	8.3	7.5	6.8	6.0	4.4
50	12.0	10.7	10.0	9.1	8.2	7.5	6.7	5.0
55	13.0	11.6	10.9	9.9	9.0	8.2	7.3	5.6
60	14.0	12.5	11.8	10.8	9.8	9.0	8.0	6.2
65	15.3	13.8	13.0	11.9	10.8	9.9	8.9	7.0
70	16.9	15.3	14.4	13.2	12.1	11.1	10.1	7.9
75	18.8	17.0	16.0	14.8	13.6	12.4	11.3	9.0
80	21.0	19.0	18.0	16.7	15.4	14.1	12.9	10.4
85	23.4	21.4	20.2	18.8	17.4	16.0	14.9	11.9
90	26.5	24.5	23.4	21.8	20.3	18.9	17.5	14.2
95	35.0	31.7	30.0	27.7	25.5	23.5	21.6	17.3
100	52.5	45.8	42.4	38.0	34.1	30.8	27.7	21.3

\* Graphically smoothed averages from Forest Products Lab. Technical Note D-5 (averages at 70 deg. F. for 5 species by M. E. Dunlap, averages at 212 deg. F. for 9 species by H. E. McKenzie, and value at 54 deg. F. for spruce by H. E. McKenzie), considered in relation to graphs of values in references (1) and (2), and criticism of values by Hawley and Wise (4).





that spruce blocks 1"x1"x6" held at 12 C. and 100% relative humidity took up 43.2% moisture in 79 days and that absorption was still taking place slowly.

In California, systematic fuel moisture measurements are not made. In view of the importance of fuel moisture, such measurements are essential to proper fire hazard rating. If not actually measured, there must be developed a formula for computing the fuel moisture content for any fuel at any time and place, through the use of detailed weather records (which are systematically kept) and their application to a formula expressing evaporation losses and condensation gains. Such a formula is now being developed, but is not presented here because the factors affecting the evaporation of moisture from woods as distinct from free water surfaces require additional study. So far as can be foretold at present, the formula seems suitable for the purpose of calculating fuel moisture contents for broad cover type classifications. The nature of the seasonal fuel moisture curve; showing fairly rapid changes for lighter fuels, but slow changes for heavy fuels, and with but little change of a cumulative nature from day to day, due to short duration of high temperatures and low humidities, tends to make the formula approximations of satisfactory accuracy. This formula will be made the subject of a separate report when completed.

### Heat factors

As already indicated, the wood must be raised from its actual temperature to the ignition point before active combustion can start. The computations required involve a fairly accurate knowledge of the specific heat of wood. Data are not plentiful. Tests of 16 species by F. Dunlap (10) for a range of temperature from 0 C. to 106 C. resulted in a mean specific heat for all species of .327, this value applying to the mean temperature of 53 C. or 127 F. The value at 0 C. or 32 F. was found to be .266. There was very little difference between species or for woods originating in various localities. Dry samples were used in the tests. Kent's Mechanical Engineers' Handbook gives values ranging from .467 to .650, but no definite particulars are given as to the conditions under which the tests were made. It seems likely that these



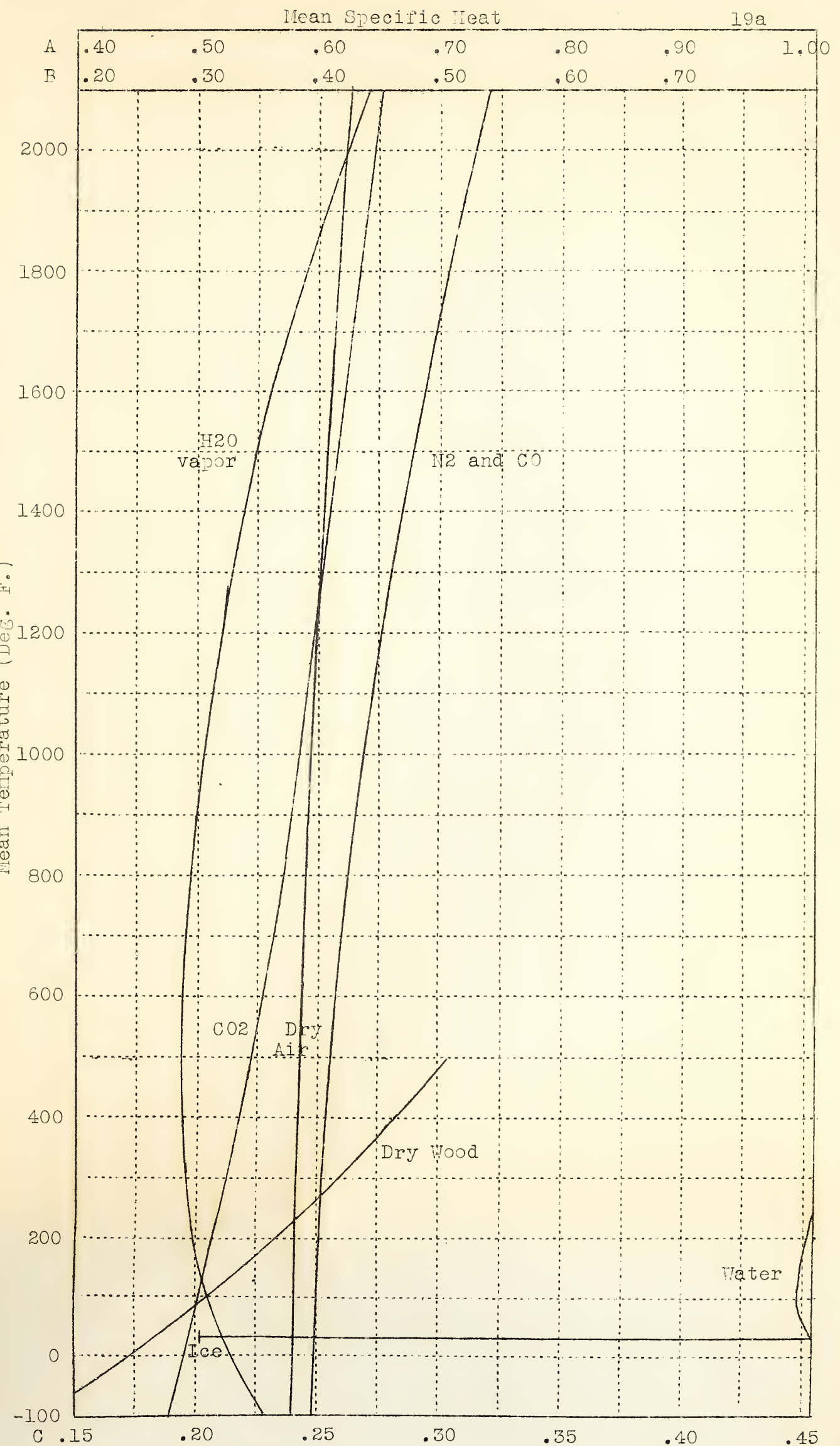


FIGURE 2 - Mean Specific Heats, in Btu per deg. F.  
 Scale A for water, ice and water vapor; Scale B for dry wood; Scale C for dry air, N<sub>2</sub>, CO and CO<sub>2</sub>.



values were for wood containing considerable moisture and therefore will not be used. Dunlap's tests indicated appreciable variation with temperature. It should be noted that Figure 2, giving curves for the mean specific heat of wood and other substances involved in combustion, uses mean temperatures. In other words, if the mean specific heat of wood for a temperature range from 40 to 540 F. is required, first find the mean temperature from the relation

$$\frac{40 + 540}{2} = 290$$

and then, using this temperature as an argument, a value of about .406 is found from the curve for the mean specific heat over this temperature range, per degree. To then find the total amount of heat required to raise the wood sample (weight one pound) to 540 F. from 40F., the following relation is used

$$W(540-40) \cdot 406 = 203 \text{ Btu}$$

where W is weight of wood (dry) in pounds. All specific heats used in this preliminary report are those for constant pressure (cp), since most of the reactions of importance may be considered to take place under atmospheric pressure (approximately constant during reaction). No allowances are made for pressures less than one atmosphere (as due to altitude, for example), since values are not much changed unless pressure differences are pronounced (1).

Ignition temperatures and heating values have already been discussed. The standard (1) values for the heats involved in changes of state of fuel moisture, in heating wood, in heating air and products of combustion, in vaporizing water and heating the vapor are as follows:

TABLE 7

Standard Values for Heat Constants

<u>Material</u>	<u>State</u>	<u>Process</u>	<u>Heat*</u>
Water.....	Solid (ice)...	heating.....	0.502
Water.....	Solid (ice)...	melting.....	143.5
Water.....	Liquid.....	heating.....	1.000
Water.....	Liquid.....	vaporization....	Table 6
Water.....	Liquid.....	boiling point....	Table 6
Water.....	Vapor.....	heating.....	Fig. 2
Wood.....	Solid.....	heating.....	Fig. 2
Wood.....	-----	ignition.....	540 F.
Wood.....	-----	heat of formation...	Table 4
Wood.....	Solid.....	heat of wetting....	30 to 35
Products of comb...	Gaseous....	heats of formation..	Table 1
Products of comb...	Gaseous....	heating,.....	Fig. 2

\* Btu unless otherwise noted.





TABLE 6  
Relations Between Elevation, Standard\* Atmosphere,  
Boiling Point and Heat of Vaporization

Elev. above sea level in feet	Approx. Air Pressure in inches	Boiling Points deg. F.	Heat of Vaporization in Btu#
-2000	32.15	215.7	968.7
-1500	31.58	214.8	969.2
-1000	31.02	213.8	969.9
- 500	30.48	212.9	970.5
0	29.921	212.0	971.2
500	29.38	211.0	971.7
1000	28.86	210.1	972.2
1500	28.32	209.2	972.8
2000	27.82	208.3	973.4
2500	27.30	207.4	973.9
3000	26.81	206.5	974.5
3500	26.31	205.6	975.1
4000	25.84	204.7	975.7
4500	25.35	203.7	976.3
5000	24.89	202.8	976.9
5500	24.41	201.9	977.5
6000	23.98	201.0	978.0
6500	23.49	200.1	978.5
7000	23.09	199.2	979.1
7500	22.63	198.2	979.7
8000	22.22	197.3	980.3
8500	21.80	196.4	980.8
9000	21.39	195.5	981.4
9500	20.98	194.6	982.0
10000	20.58	193.7	982.6
10500	20.18	192.8	983.1
11000	19.79	191.8	983.7
11500	19.40	190.9	984.3
12000	19.03	190.0	984.9
12500	18.64	189.1	985.4
13000	18.28	188.1	986.0
13500	17.92	187.2	986.5
14000	17.57	186.3	987.1
14500	17.21	185.4	987.7
15000	16.85	184.4	988.3

# Btu: British thermal units, defined at 60 F.

\* Standard atmosphere as adopted by the National Advisory Committee for Aeronautics, with specifications as follows: Sea level pressure 29.921" F.

Sea level temperature 59 F.

Temperature gradient 0.003566 F. per ft.

Temperature in stratosphere -67 F.

Altitude at base of stratosphere 35,332 Ft.

The air is a dry, perfect gas.





For the curve of mean specific heat of dry wood in Figure 2, Dunlap's values were used as two points on the curve, and since wood decomposes gradually with increased temperature (evolving volatile materials and becoming practically pure carbon or charcoal), the mean specific heat of carbon at 870 F. was taken from the International Critical Tables (1) as a third point on the curve. The result is plotted in Figure 2.

### DERIVATION OF FORMULAE

The foregoing preliminaries disposed of, the following discussions will indicate the methods used and attempted to secure mathematical expressions of the various factors involved in fire hazard rating, and to combine factor expressions into general formulae. This work is not complete, but is believed to be suggestive of general method. In some cases, the mathematical formulae derived can be said to be in definite and final form. In developing the formulae, the additional discussion required for adequate understanding of the effects of modifying influences, not covered in the foregoing, and the discussion necessary to clarify methods, define units and indicate assumptions, will appear wherever it seems needed.

#### Fundamental bases

Tentatively, the unit of fuel considered will be a cube with a density corresponding to that for pure wood substance (1.47) to which all types of fuel will be referred. The cube will be considered to be freely suspended in air containing no appreciable foreign materials (dust, smoke particles, etc.) and no products of combustion as such. The system of units used will be English, with lengths in feet and miles, time in seconds, areas in square feet and square miles, volumes in cubic feet, weights in avoirdupois pounds (later tons), temperatures in degrees Fahrenheit, barometric and vapor pressures in mercurial inches and heats in British thermal units, defined at 60 F. Table 8 on page 21a lists the symbols employed in the formulae. Since many contain more than one letter, it should be understood that mere juxtaposition of symbol letters does not necessarily indicate multiplication, as in ordinary mathematical formulae. To indicate this operation, spaces usually are left between symbols containing more than one letter. Hazard of fire inception and translation will be considered partially, but only inception hazard will be developed to a degree warranting the statement of a formula of general type. It is assumed that wood substance is not heated until all water is driven off, and that ignition cannot be accomplished similarly until the wood is "bone" dry, in both cases considering a limited surface only.



TABLE 8  
Symbols used in Formulae.

Ab: area burning surface, or fire area, square feet.  
 Ac: cross sectional area of "smoke" column, sq. ft.  
 Aes: exposed surface fuel area, square feet, also sq.mi.  
 a: acceleration; also a fire dimension, parallel to prevailing wind.  
 B: air pressure in general, inches of mercury.  
 Ba: total air pressure, inches.  
 Bv: vapor pressure.  
 Btu: British thermal unit, a measure of heat quantity, defined at 60 F.  
 C: carbon.  
 C%: percentage by weight of carbon per pound of dry fuel.  
 C.: Centigrade.  
 CO: carbon monoxide.  
 CO<sub>2</sub>: carbon dioxide.  
 Cf: circumference of fire (perimeter) in feet.  
 cos: natural trigonometric cosine of an angle.  
 cp: constant pressure.  
 Da: density of air (any units, commonly weight in lbs. per cu.ft. or in grams per liter).  
 Dc: density (virtual) of mixture of gases in "smoke" column.  
 Df: true oven dry density of fuel, referred to the weight of pure water (62.428 lbs.) per cu.ft. at its maximum density (4 C. or 39.2 F.).  
 E: eddy or whirl. F.: Fahrenheit.  
 FM%: fuel moisture percentage (% given by weight of water divided by oven dry weight of wood).  
 g: acceleration of gravity, 32.174 ft. per sec. per sec.  
 G: slope angle between ground and horizontal.  
 G%: same, but in percent of grade.  
 G: gram weight.  
 Hf: heat of fusion (melting), Btu, per lb. ordinarily.  
 Hv: heat of vaporization, Btu, per lb., ordinarily.  
 HI: hazard of fire inception in relative units.  
 HVi: effective heating value of any given ignition agent, in Btu.  
 HF: heat of formation in Btu per lb., ordinarily.  
 H: hydrogen.  
 H%: percentage by weight of hydrogen per lb. of dry fuel.  
 H<sub>2</sub>O: water, liquid or vapor.  
 HV: heating value in Btu, total or per lb. of dry fuel.  
 HIG: heat required for ignition, total; total or per lb. of dry fuel.  
 Hw: heat of wetting, in Btu per lb. of dry fuel.  
 I: indraft in general.  
 K, k, k<sub>1</sub>, k<sub>2</sub>: constants.  
 mm.: millimeters.  
 N<sub>2</sub>: nitrogen.  
 O: oxygen.  
 O%: percentage by weight of oxygen per lb. of dry fuel.





CONTINUED

RH: relative humidity %.  
 R: resultant.  
 s: slope angle between "smoke" column and horizontal.  
 s%: same, but in % grade.  
 sin: natural trigonometric sine of an angle.  
 SHf: mean specific heat of fuel, in Btu per lb. per deg.  
 SHs: mean specific heat of solid (ice) as above.  
 SHw: mean specific heat of liquid water, as above.  
 SHv: mean specific heat of water vapor, as above.  
 SHa: mean specific heat of air, as above.  
 T: temperature in general, absolute or Fahrenheit. If absolute, expressed by  $459.6 + T$  (Fahrenheit).  
 Ta: air temperature, Fahrenheit degrees.  
 Tw: temperature of fuel moisture or water, F.  
 Tb: temperature of boiling point of water, F.  
 Ts: temperature of solid (ice), F.  
 tan: natural trigonometric tangent of an angle.  
 Ti: ignition temperature, F.  
 Tf: fuel temperature, actual, F.  
 Tm: temperature of melting point of ice, F.  
 Tc: temperature of "smoke" column at its base, F.  
 Vwi: fire-produced indraft wind velocity, feet per sec.  
 Vwp: outside prevailing wind velocity, undisturbed by fire-produced indrafts, in feet per sec.  
 Vws: velocity of wind parallel to a slope, feet per sec.  
 Vwa: corrected wind velocity as indicated by a cup anemometer, ft. per sec.  
 Vpc: volume of products of combustion, cubic feet, or combustion layers of cross section equal to fire area and depth y.  
 Vf: volume of fuel, cu.ft.  
 Va: volume of air, cu.ft.  
 Vv: volume of vapor, cu.ft.  
 VP: vapor pressure, inches, in general.  
 Vr: a resultant velocity in ft. per sec.  
 Vc: vertical component of ascent velocity of "smoke" column, ft. per sec.  
 Vw: horizontal or slope component of "smoke" column, wind, or wind velocity in general, in ft. per sec.  
 Vw: a rate of air supply, based on wind velocity, but including effects of fire shape, size, ground slope, corrected anemometer reading and depth of combustion layer y.  
 Vmph: velocity miles per hour. Vfps: velocity feet per sec.  
 Wacc: weight of air required for complete combustion, total or per lb. dry fuel.  
 Wfo: weight of fuel oxygen, total or per lb. dry fuel.  
 Wo: weight oxygen; in general, lbs. per cu.ft. of air.  
 Wa: weight of air, as above, dry or moist.  
 Wf: weight of fuel, dry, lbs. or tons.  
 Ww: weight of fuel moisture or water (any form), lbs.  
 W: wind in general.  
 x: a cross sectional dimension of the "smoke" column parallel to the prevailing wind, feet; also indicates multiplication.  
 y: thickness (ft.) of air layer adjacent to burning surface in which combustion is active.  
 z: fire dimension at right angles to prevailing wind, ft.





### The amount of heat required for ignition

Hawley's calculation given on page 15 apparently does not include all of the principal factors involved. To cause one pound of standard wood fuel to ignite, assuming a fixed ignition point temperature of 540 F., requires the following:

- 1.) Heat to raise dry wood from its actual temperature to the ignition temperature.
- 2.) Heat to drive off all fuel moisture. If in the form of ice, the successive stages are
  - a.) Heat ice to melting point.
  - b.) Melt ice.
  - c.) Heat water from melting point to boiling point.
  - d.) Vaporize water.
  - e.) Heat vapor to ignition point.

If the fuel is already above the freezing point, and the fuel moisture is consequently liquid water, the ice stages A. and b. need not be considered, and the actual temperature of the water instead of the melting point is considered in stage c.

- f.) Heat to overcome the chemical attraction between the wood and water, approximately 30 Btu per pound of dry hardwood and 35 Btu for conifers (from values by Dunlap and from the International Critical Tables), termed the "heat of wetting".

3.) Heat required to raise the air needed for combustion from its actual temperature to the ignition temperature. Obviously, the chemical combination between the fuel substances and the oxygen of the air does not occur in the sense of active combustion until the ignition point is reached; both the fuel substances and the oxygen must attain this temperature if the ignition temperature is to be maintained during combustion and not merely for an instant at the start of combustion; and since the oxygen is thoroughly mixed with other elements (principally nitrogen) in the air, the whole air mass must be heated and not the oxygen alone.

Obviously, one pound of wood does not necessarily represent the real unit involved in ignition, especially for different igniting agents, which may vary from very small surfaces (practically points) to rather extensive areas (as with ignition by radiated heat). The relative amounts of heat involved remain unchanged regardless of the fundamental unit adopted. The pound is used because it is the most convenient unit for computations.



The amount of heat required to raise any substance through any temperature range is given by the general relation:

- 1) Weight substance (final temp. - initial temp.) mean specific heat of substance per degree = amt. heat.

The amount of heat is expressed in Btu if weights are in pounds, temperatures in degrees Fahrenheit and mean specific heats in Btu per degree.

From the foregoing equation and the discussion on page 22, using symbols as on page 21a, the total heat (HIG) required for ignition of standard dry wood fuel (of composition as in Table 8) is expressed by the relation:

$$2) \text{ HIG} = W_f [SH_f(T_i - T_f) + H_w] + W_w [SH_s(T_m - T_s) + H_f + SH_w(T_b - T_w) + H_v + SH_v(T_i - T_b)] + SH_a(T_i - T_a)W_a$$

The relative hazard of fire inception obviously is inversely proportional to the amount of heat required for ignition, other factors the same, or

$$3) \text{ HI} = \frac{1}{\text{HIG}} \quad \text{and other factors.}$$

It is apparent that all igniting agents acting through flame or glowing sparks, rather than mere heat, are subject to the identical conditions that govern fire behavior. Under certain conditions, an igniting agent may be ineffectual due to its inability to deliver a sufficient amount of heat per unit time per unit fuel area, over and above losses of various sorts. It seems possible to definitely evaluate the relative fire inception power of various igniting agents under different conditions, if suitable provision can be made for heat lost by radiation, conduction and convection, and for the total heating value as well as the rate of combustion of the materials composing the igniting agent. Assuming that this can be done, the effective heating value of the igniting agent (HVi) affects formula 3 as follows:

$$4) \text{ HI} = \frac{\text{HVi}}{\text{HIG}} \quad \text{and other factors.}$$

In other words, if the effective heat produced by the igniting agent is less than that required for ignition, a low hazard exists; if HVi is equal to HIG, unit hazard occurs, and if HVi is greater than HIG, a hazard greater than unity ~~is~~ occurs. This report, however, will



not attempt rating of igniting agents. This matter will be deferred to later progress reports.

#### The amount of heat produced by complete combustion

This is merely the total heating value of a given quantity of a given fuel, the unit value being based on careful calorimeter measurements. Given types of fuel may be considered to have certain average heating values (dry), sufficiently accurate for fire hazard rating purposes, where other possible sources of error are many. The amount of heat produced by combustion (HF) is expressed by

$$5) \quad HF = Wf(HV)$$

for complete combustion and lesser values in proportion to the completeness of combustion and the nature and amount of products formed.

Some of the HF is utilized in driving off fuel moisture, some heats the fuel, some heats the soil, some heats air for combination with fuel, some heats the products of combustion and some is radiated to objects at a distance. After the igniting agent has expended its store of heat and has started combustion, the HF must be so dissipated that the fuel adjacent to the surface actually burning is kept continuously at or above the ignition temperature. It is apparent that the characteristics of the substances and the processes involved must be considered in some detail, and that the rate of evolution of the heat (directly proportional to the speed of the reaction) must be considered also in determining the relative heat losses by radiation, conduction and convection. Only a part of this problem will be discussed later in this report; further attack will be postponed to further progress reports.

#### The amounts of air required for combustion

Dulong's formula for the heating value of given fuels has the general form:

$$6) \quad HV \text{ or } HF = Wf \left[ k_1 C\% + k_2 \left( H\% - \frac{O\%}{8} \right) \right]$$

when a part of the hydrogen in the fuel is considered to be already, in effect, combined with fuel oxygen. The Dulong relation uses values of 1 and 16, respectively, for the atomic weights of hydrogen and oxygen. More accurately, the atomic weight of hydrogen is 1.0077, which makes the divisor of the oxygen percentage about 7.94 instead of 8. With this correction, the Dulong formula can be used to calculate the amounts of air required for combustion, by substituting suitable values from Table 1 for the constants  $k_1$  and  $k_2$ .





From Table 1, 7.94 lbs. of oxygen are required for complete combustion of one lb. of hydrogen, and 2.67 lbs. for one lb. of carbon. When combustion of the latter is incomplete, only 1.33 lbs. of oxygen are required. As will be shown later, oxygen constitutes .23197766 lb. in each pound of dry air free from foreign materials and not mixed with products of combustion. Assuming perfect contact of air with fuel, the weights of dry air required for combustion per pound of combustible, are as follows:

$$7) \quad W_a \text{ (for H)} = \frac{7.94}{.23197766} = 34.23 \text{ lbs. (H}_2\text{O product)}$$

$$8) \quad W_a \text{ (for C)} = \frac{2.67}{.23197766} = 11.50 \text{ lbs. (CO}_2\text{ product)}$$

Foregoing for complete combustion.

$$9) \quad W_a \text{ (for C)} = \frac{1.33 \text{ plus}}{.23197766} = 5.75 \text{ lbs. (CO product)}$$

Foregoing for incomplete combustion.

The density of air of any moisture content, when referred to dry air under standard conditions as unity, is given by

$$10) \quad D_a = \frac{6.215(2.643B_a - B_v)}{459.6 + T_a}$$

According to the International Critical Tables (1) and Humphreys (11) the weight of dry air under standard conditions is .08072 lbs. per cu.ft. The weight of dry air under any conditions of temperature, pressure and relative humidity is given by the equation

$$11) \quad W_a = \frac{.08072(491.6)(B_a - B_v)}{29.921(459.6 + T_a)}$$

which simplifies to

$$12) \quad W_a = \frac{1.32625(B_a - B_v)}{460 + T_a}$$

since the volume of dry air in a unit volume of moist air mixture is given by

$$13) \quad V_a = \frac{B_a - B_v}{B_a}$$

and the volume of water vapor, similarly, by

$$14) \quad V_v = \frac{B_v}{B_a}$$





The volume of moist air required for complete combustion is expressed by the following equations, since the volume is given by total weight of dry air required divided by the weight of dry air per cubic foot of mixture:

$$15) V_a \text{ (for H)} = \frac{34.23(460+T_a)}{1.32625(B_a-B_v)} = \frac{25.814(460+T_a)}{B_a-B_v}$$

$$16) V_a \text{ (for C)} = \frac{11.50(460+T_a)}{1.32625(B_a-B_v)} = \frac{8.673(460+T_a)}{B_a-B_v}$$

when combustion is complete, and

$$17) V_a \text{ (for C)} = \frac{5.75(460+T_a)}{1.32625(B_a-B_v)} = \frac{4.386(460+T_a)}{B_a-B_v}$$

when combustion is incomplete. The foregoing give values for each pound of combustible. Using Dulong's formula, values for a given fuel of known chemical composition are given by the following equations:

$$18) W_a = W_f \left[ 34.23(H\% - \frac{0\%}{7.94}) + 11.50C\% \right]$$

for complete combustion, and

$$19) W_a = W_f \left[ 34.23(H\% - \frac{0\%}{7.94}) + 5.75C\% \right]$$

for incomplete combustion, a part of the oxygen used in combustion in each case being supplied from the fuel.

$$20) V_a = W_f(460+T_a) \frac{5.239(7.94H\% - 0\% + 2.67C\%)}{B_a-B_v}$$

(Complete combustion)

$$21) V_a = W_f(460+T_a) \frac{5.239(7.94H\% - 0\% + 1.33C\%)}{B_a-B_v}$$

(Incomplete combustion)

The substitutions on which equations 18 to 21 are based involve equations 6, 12, 15, 16 and 17.

If  $\overline{V_w}$  is the true wind velocity in feet per second, then the weight or volume of air supplied in unit time is given by

$$22) \text{ Total } W_a \text{ or } V_a = \overline{V_w}(W_a \text{ or } V_a).$$

### Oxygen supply

It has been suggested by Hawley (6) and again by Gisborne (7) that differences in oxygen supply as af-



affected by displacement of air through the action of water vapor and products of combustion may affect fire behavior materially, and that further investigation of this matter is desirable to determine its importance. The following analysis attempts to definitely evaluate the oxygen supply factor in extension of the air supply discussion already given.

### Factors

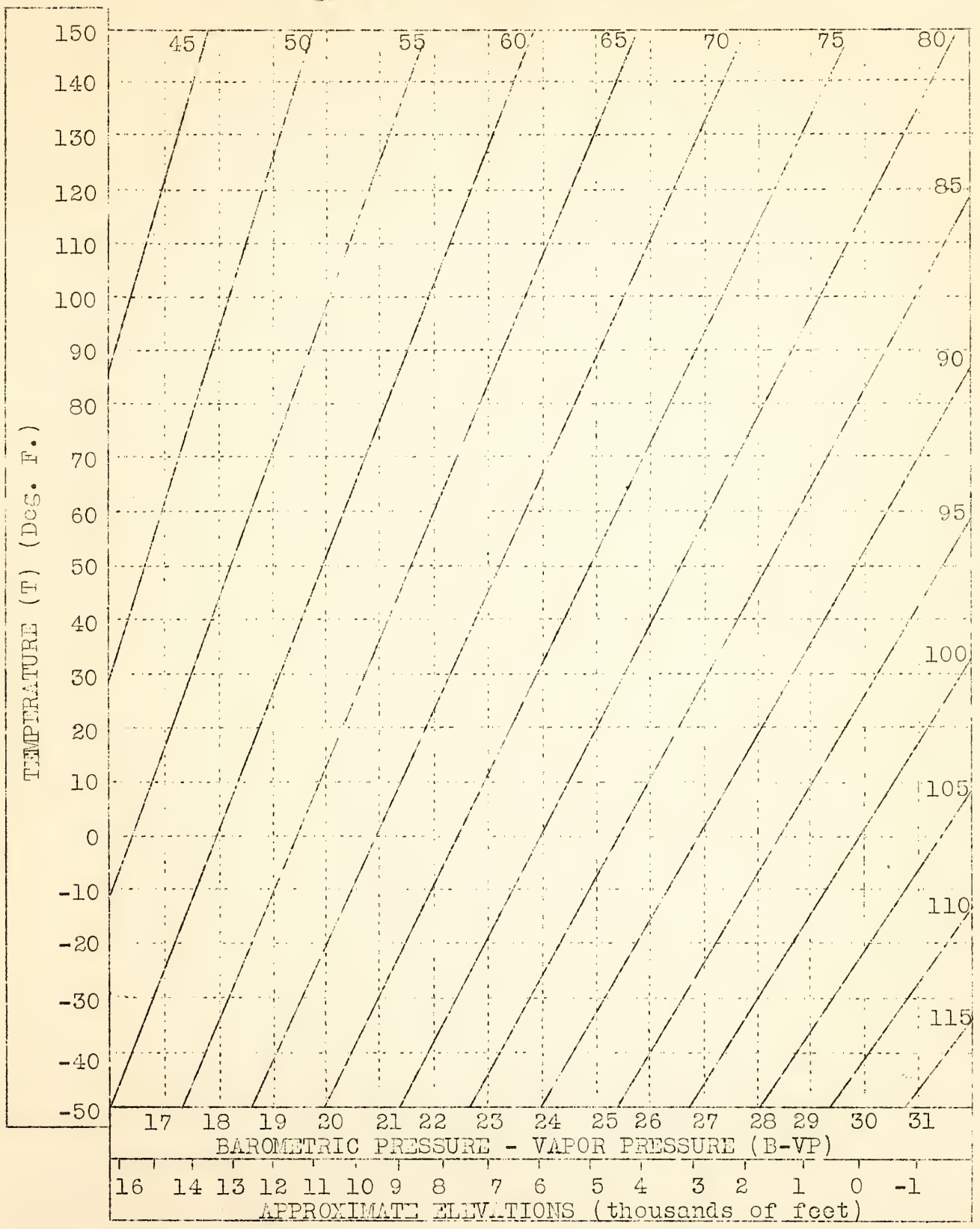
The factors controlling oxygen supply, so far as practical fire hazard rating is concerned, may be listed as follows:

- The effective oxygen supply is dependent on
- 1.) The amount of oxygen per unit air volume.
  - 2.) The rate of supply of unit air volumes.
  - 3.) The degree of effective contact between the oxygen and burning fuel surfaces.
- 1.) The amount is affected by
    - a. Air density-controlled primarily by temperature and pressure.
    - b. The percentage of oxygen in air-controlled by the displacement of air by water vapor and foreign materials already in the air, the nature of the air mixture and displacement by products of combustion ( $H_2O$ ,  $N_2$ ,  $CO$ ,  $CO_2$ , heat and smoke particles).
  - 2.) The rate of supply is dependent on
    - a. Number of unit volumes supplied in unit time-controlled by indrafts produced through the temperature differential between gases in contact with burning fuel surfaces and outside air, and by general prevailing wind movement or velocity.
  - 3.) The contact with fuel is affected by
    - a. The ratio of exposed (burning) fuel surface to oven dry fuel volume, determining the area in contact with air, which for unit volume becomes simply the surface area, and
    - b. The ratio of exposed surface to mass or quantity of fuel, since various woods have different gross densities, and therefore differing amounts of wood substance are exposed to air contact per unit surface area.



27a

FIGURE 2a  
WEIGHT OF OXYGEN PER CUBIC FOOT OF AIR  
(slanting lines) in percentages of weight (0.02 lbs.)  
at 2 deg. F. and 30" net air pressure.







- c. Fuel moisture content- assuming that any water in fuel prevents contact with air until driven off by heat.

### Amount

According to the International Critical Tables (1) and Humphreys (11), the oxygen in the air is merely mechanically mixed with other gases and is not chemically combined with them (other than a small amount of CO<sub>2</sub>) in any way. Oxygen amounts to 20.99% by volume in dry air. The percentage variation with altitude is negligible for practical purposes, being nearly constant (for dry air) below about 36,000 ft. Reference (1) gives densities for dry air and oxygen under standard conditions (temperature 32 deg. F., pressure 29.921" and relative humidity 0%) as follows:

DRY AIR: 1.293 g. per liter or .08072 lbs. per cu.ft.  
OXYGEN: 1.429 g. per liter or .08921 lbs. per cu.ft.

If the value for dry air represents unit density, then oxygen has a density relative to dry air, as given by

$$\frac{1.429}{1.293} = 1.1051818$$

and the percentage of oxygen by weight per unit volume of dry air is given by

$$20.99 \times 1.1051818 = 23.197766\%$$

This percentage is equivalent to .018725237 lbs. of oxygen per cubic foot of standard dry air. In accordance with the gas laws (assuming that the air and oxygen behave strictly as perfect gases, which they do practically at ordinary temperatures and pressures), the density of air (or oxygen) varies inversely with the absolute temperature and directly with the pressure, and hence the weight per cubic foot of dry air under any conditions of temperature and pressure may be expressed by the equation:

$$23) \quad W_o = \frac{.018725237(491.6)Ba}{29.921(459.6+Ta)}$$

Fahrenheit temperatures being expressed on the absolute scale by the addition of 459.6, which is the equivalent of the value for absolute zero (-273.13) given by Humphreys (11), converted to Fahrenheit zero. Equation 23, simplified, becomes:



$$24) \quad W_o = \frac{.3076543B_a}{459.6 + T_a}$$

The volume of water vapor and of air present per cubic foot of moist air mixture has already been expressed by equations 13 and 14. Since water vapor is not dissociated into free (chemically uncombined) hydrogen and oxygen except at very high temperatures (only 1.8% dissociation at 3600 F.), for practical purposes it may be considered to displace an equivalent volume of dry air, and hence reduce the amount of oxygen per unit volume of moist air mixture. The formula for  $W_o$  per cubic foot of air mixture under any practical conditions of temperature, pressure and relative humidity becomes

$$25) \quad W_o = \frac{.3076543B_a(B_a - B_v)}{B_a(459.6 + T_a)}$$

which simplifies to

$$26) \quad W_o = \frac{.308(B_a - B_v)}{460 + T_a}$$

with a more than sufficient degree of practical accuracy. Figure 2a on page 27a is a graph of this equation. From this figure, it is evident that at a temperature of 80 F. and not pressure of 30" at sea level, that the relative amount of oxygen per cubic foot of air is 85.5%, and that under the same conditions of temperature and relative humidity but at an elevation of 6000 ft. the relative amount of oxygen is 68.5%. Other things being equal, it may be said that the rate of the combustion reaction (and of fire spread) varies directly with oxygen supply; hence

$$\frac{\text{sea level } 85.5\%}{6000 \text{ ft. } 68.5\%} = 125\%, \text{ nearly,}$$

which means that a fire at sea level would burn 25% faster than one at 6000 ft. under the same conditions except for oxygen supply. Similar calculations can be made for any other conditions or levels.

Foreign materials already in the air (prior to combustion) may consist of dust particles, fog and cloud water droplets, or rain drops and snow flakes, among others less consequential. The atmospheric water vapor has already been taken care of in the  $W_o$  formula, and while the percentage of  $CO_2$  fluctuates slightly, the range is not consequential in affecting air density. In general, foreign materials constitute such a very small proportion of the air mixture that they can be disregarded. This is demonstrated by a calculation based on a table by Humphreys (11, page 267) from which it is found that the volume of air displaced by falling rain during a cloudburst (temp. 0 C., pres. 740 mm., rate of precipitation approximately 4" per



hour) would amount to but .00000054 cu. ft. per unit air volume. Hence all corrections for the presence of foreign materials other than water vapor and products of combustion may be disregarded.

The products of combustion ( $H_2O$ ,  $N_2$ ,  $CO$ ,  $CO_2$ , smoke and heat) must be considered, however. All of the gases produced by combustion are incombustible (except  $CO$  when combustion is incomplete). The oxygen in the products is chemically combined and is of no further importance in affecting combustion except by air displacement. It may be questioned whether the smoke particles (fragments of unburned fuel, principally carbon) are sufficient in number and large enough in size to affect air displacement materially; and certainly not more important than the cloudburst calculation already cited (dense fog is less consequential). Therefore, it seems reasonable to suppose that it is only the purely gaseous products of combustion that importantly affect air displacement. The heat produced by combustion results in decreased density of nearby air masses and consequently less available oxygen per unit volume.

At the start of combustion, the burning surface is at the ignition temperature, and the air necessarily must be heated to this temperature prior to the combination of its oxygen with fuel constituents. After combustion is under way, however, due to the surplus heat released by the combustion process, the burning surface may have a very much higher temperature. There thus enters the question of the proper temperature to use in the oxygen supply formulae; this temperature, apparently, is that of the burning surface.

It will be necessary, therefore, to secure a formula expressing the temperature of the burning surface under various conditions, and substitute it for  $T_a$  in the oxygen formulae, in order to adapt the latter to actual combustion conditions. This burning surface temperature is approximately equivalent to the temperature at the base of the column of ascending products of combustion (the "smoke" column), and a formula for determining this temperature,  $T_c$  will be given later.

Since wood will not burn until all water is driven from a given limited surface, the question of displacement of air by fuel moisture becomes a question of the amount of water vapor added to the products of combus-





FIGURE 3

## RELATIONS BETWEEN FIRE AREA AND PERIMETER

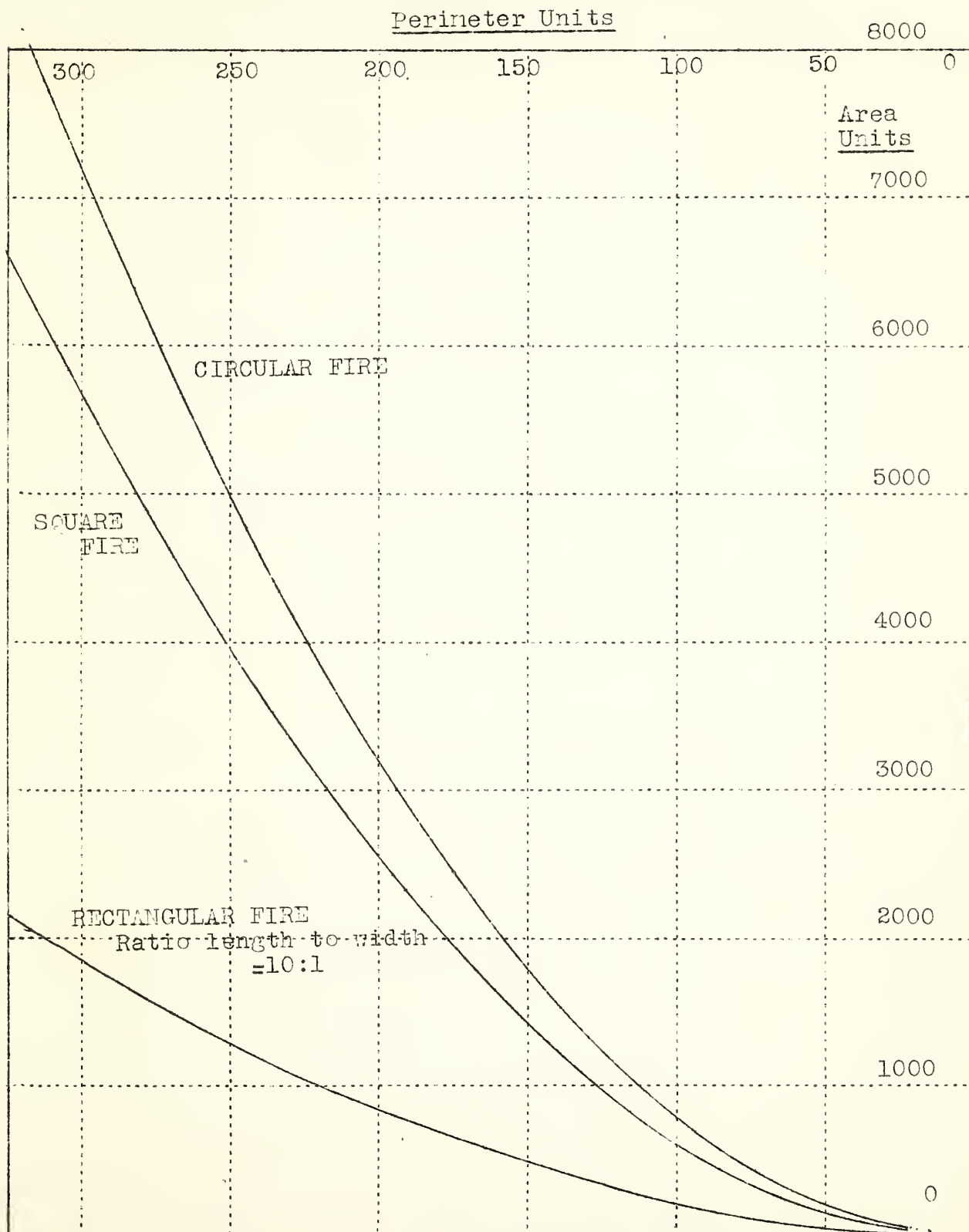
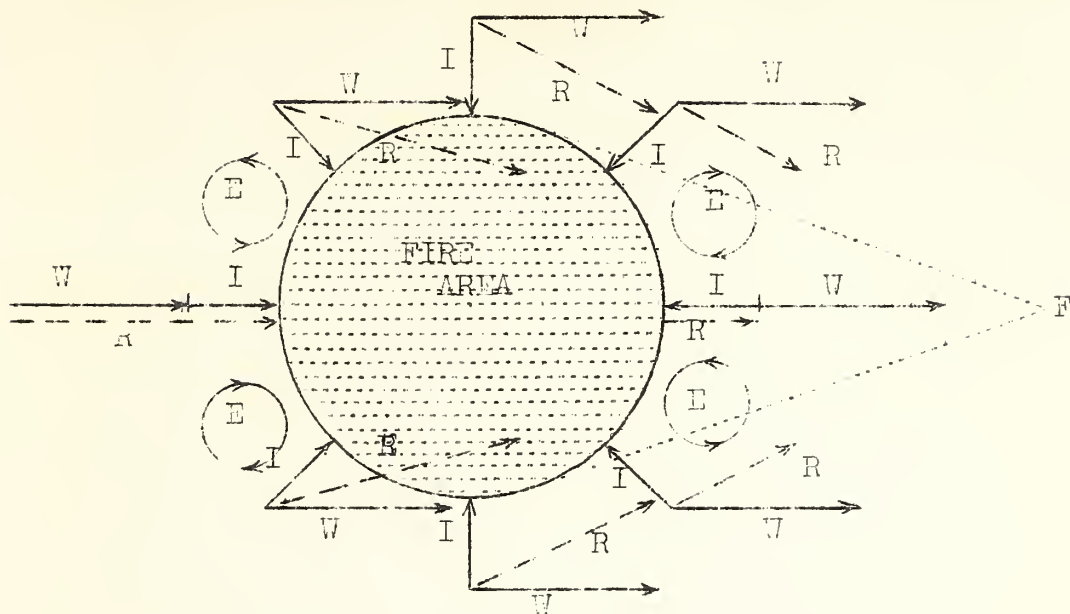
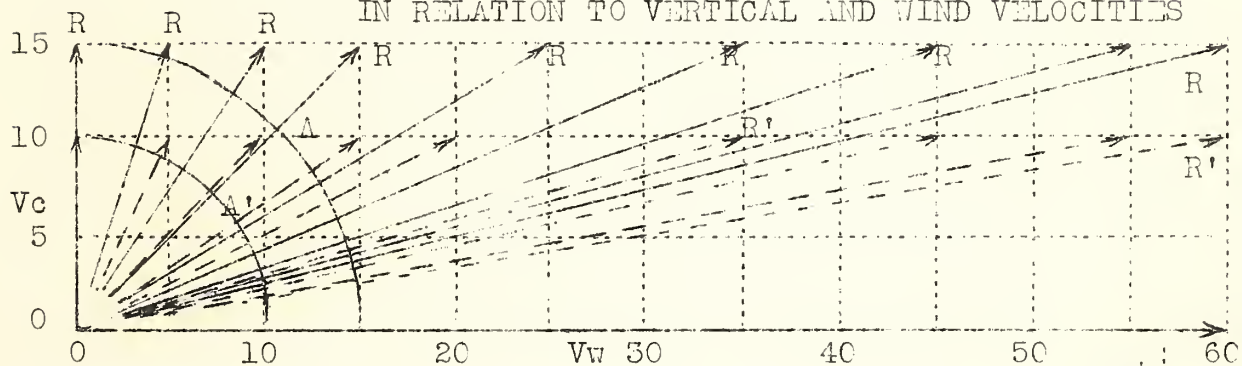
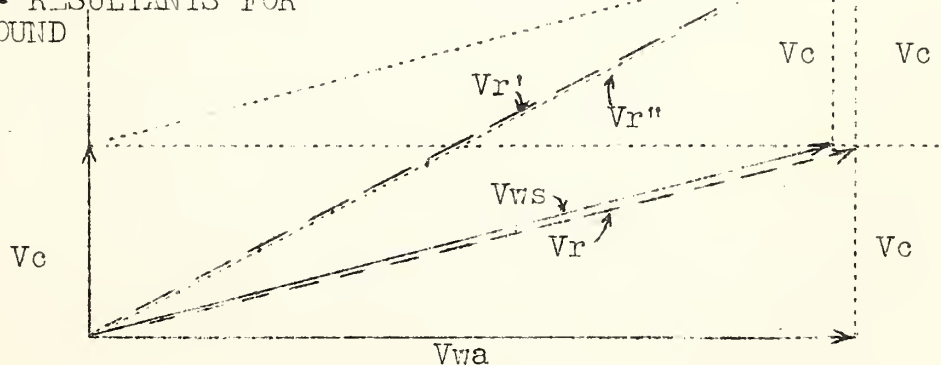








FIGURE 4 - FIRE WIND RESULTANTS AT SURFACE

FIGURE 5 - RESULTANT DRIFT OF SMOKE COLUMN  
IN RELATION TO VERTICAL AND WIND VELOCITIESFIGURE 5a - RESULTANTS FOR  
SLOPING GROUND





In the figures,  $a$  is a dimension of the fire parallel to the prevailing wind direction,  $s$  is the slope angle between the "smoke" column and the horizontal,  $g$  is a similar slope angle between the horizontal and the ground,  $x$  is a cross sectional dimension of the "smoke" column,  $V_{wp}$  is the prevailing wind and  $V_{wi}$  the indraft velocities,  $V_r$  is a resultant velocity of the column, with components  $V_c$  (vertical column velocity) and  $V_w$  (prevailing wind velocity), all shown as vectors. The actual wind affecting a given part of a fire is a resultant of the general prevailing wind and an indraft component, as shown in Figure 4, the indraft being proportional to the density differences between the air at temperature  $T_a$  and the "smoke" column gases, at temperature  $T_c$ . The resultants shown in Figure 4 actually apply to points on the fire circumference (and not to points outside, as drawn for clearness). Obviously, the effect of air displacement by products of combustion is important only in a layer adjacent to the burning surface. The thickness of this layer is important in connection with air displacement, as will be shown later, but cannot be evaluated at present and hence will be given by the symbol  $y$ . The  $V_r$  of the column is a measure of the volume of gases leaving the burning surface in unit time, when considered in conjunction with the cross sectional area of the column, related in turn to the burning area by the slope angle. The volume obviously depends closely on the fire shape. In the following formula derivation, a simple square fire will be assumed, with side dimension  $a$ . Hence, the cross sectional area of the column becomes  $xa$ , a rectangular shape. For level ground, obviously,

$$x = a \sin s$$

For sloping ground, it can be shown that

$$x = a \sin (s - g)$$

The cross sectional column area for sloping ground is  $xa$ , or

$$A_c = a^2 \sin (s - g)$$

The volume of a unit layer of thickness  $y$ , for the fire area itself, is  $a^2y$ . Obviously, the thickness of the layer when the cross section is not the fire but the column area, becomes

$$\frac{a^2y}{a^2 \sin (s-g)}$$



The volume of the products of combustion evolved in unit time obviously is

$V_{pc} = A_c V_r$ , which is equal to

$a^2 \sin (s-g) V_r$ , which is equal to

$$a^2 \sin (s-g) \frac{V_{wp}}{\cos s}$$

for any ground slope, since the velocity of the wind (blowing parallel to the ground slope) is given by an anemometer exposed plumb in terms of a horizontal velocity and not a slope velocity. The number of layers of volume equal to the volume for the fire area and depth  $y$ , is given by

$$\frac{a^2 \sin (s-g) \frac{V_{wp}}{\cos s}}{\frac{a^2 y}{a^2 \sin (s-g)}}$$

which simplifies to

$$\frac{a^2 \sin^2(s-g) V_{wp}}{y \cos s}$$

representing the number of layers at temperature  $T_c$ .

At the same time, air is being fed into the fire by the prevailing wind (slope velocity, not horizontal projection) and by the indraft, as shown in the lower figure on page 31. For a simple fire, the indraft may be assumed to be equal on all sides (disregarding for the time being the effect of ground slope in accelerating or retarding air flow at the upper and lower parts of the fire, when on sloping ground, by increasing or decreasing the slope velocity component due to the effect of gravity, over and above the component due to density differences between the column and the air), and proportional to density differences. The volume of inflow due to the prevailing (slope) wind may be considered to be given by

$$V_{wp} (\text{slope}) y z$$

where  $z$  is a fire dimension given by the projection of the fire area on a straight line at right angles to the prevailing wind direction, the volume being appropriate to the temperature  $T_a$ . The number of layers of thickness  $y$  and fire area  $a^2$  is given by



$$\frac{V_{wp}(\text{slope}) y z}{a^2 y} \quad \text{which reduces to}$$

$$\frac{V_{wp}(\text{slope})}{a} \quad \text{for a square fire, when the}$$

wind blows parallel to a side. This represents the number of layers fed in unit time by the prevailing wind only. The indraft similarly may be considered to feed air inward to the fire area along the entire fire circumference, the volume being given by

$V_{wi}(y) 4a$  for a square fire with side dimension  $a$ , and the number of layers of thickness  $y$  and equal to the fire area in cross section is given by

$$\frac{V_{wi}(y) 4a}{a^2 y} \quad \text{which reduces to}$$

$$\frac{4V_{wi}}{a}$$

This number of layers due to indraft is additive to the number brought in by the prevailing wind, and hence the total number of layers of air fed into the fire by both indraft and prevailing wind becomes

$$\frac{V_{wp}(\text{slope})}{a} + 4V_{wi}$$

Without considering the effect of slope on the indraft velocities of a simple, regular fire area (the effect is compensating), the true slope velocity of the prevailing wind, when the direction is directly up or down slope and not at some other angle, is given by

$$\frac{V_{wp}}{\cos g} \quad (\text{by anemometer})$$

making the foregoing equation

$$\frac{V_{wp}(\text{anem.}) + 4V_{wi} \cos g}{a \cos g}$$

Parenthetically, it should be noted that if a fire on level ground is square, the shape of the column is rectangular under other than calm conditions, and if the fire is elliptical, the column may be circular, and vice versa.

The number of layers (or volume) of air is increased on mixing with the "smoke" column gases by the expansion due to change of temperature from  $T_a$  to  $T_c$ , so that the





foregoing equation becomes

$$27) \quad \frac{(460+T_c)[V_{wp}(\text{anem.}) + 4V_{wi} \cos g]}{(460+T_a)a \cos g}$$

thus making the air volume directly comparable with the volume of products of combustion, both at temperature  $T_c$ .

The proportion of air in the mixture of air and volatile wood or combustion products appears to be given, then, by the following equation, if combustion is incomplete or complete:

$$28) \quad \frac{(460+T_c)[V_{wp} + 4V_{wi} \cos g]}{(460+T_a)a \cos g} \cdot \frac{a^2 \sin^2(s-g)V_{wp}}{y \cos s}$$

This merely indicates the proportion of air layers of given volume to similar layers of combustion products (including the air), considering that the air supply from outside sources near the ground is not mixed (outside the fire area itself) with smoke or products of combustion. The relation is a coefficient or multiplier of the oxygen supply formula 26, when the latter is altered to indicate the number of cubic feet of air supplied to the fire of given shape and under given conditions in unit time.

Equation 28 simplifies to

$$29) \quad \frac{(460+T_c)[V_{wp} + 4V_{wi} \cos g] y \cos s}{(460+T_a) \cos g a^3 \sin^2(s-g)V_{wp}}$$

It is apparent from the foregoing that the displacement or mixing of air will vary considerably with fire shape, fire orientation, wind velocity and thickness of the layer ( $y$ ) in which active combustion occurs. Evaluation of  $y$  may be possible through other relations to be developed in later reports, or from field observations of flame heights. Evaluation will not be attempted in this report, and the relations given are merely suggestive of possible attacks on the problem of air displacement.

If  $A_c$  is cross sectional area of "smoke" column,  $A_b$  is the fire area,  $y$  is the depth of layer in which combustion is active,  $z$  is a dimension of the fire at right angles to the prevailing wind direction,  $V_{wp}$  is the true prevailing wind velocity (considering slope and orientation effects) and  $C_f$  the fire circumference,





a general form of equation 29, for any fire shape, orientation and ground slope, may be expressed as

$$30) \quad \frac{y (zV_{wp} + C_f V_{wi}) (460 + T_c)}{A_c V_r (460 + T_a)}$$

### Rate

Returning again to the question of oxygen supply, as already indicated  $T_c$  must be substituted for  $T_a$  in formula 26. In addition, for any given fire shape, area and other conditions, a certain volume of air is fed into the fire, this volume being given by

$$zyV_{wp} + yC_f V_{wi} \quad \text{in general terms, and for}$$

the square fire assumed in prior derivations

$$ayV_{wp} + 4 ayV_{wi}$$

In general terms, since formula 26 gives the weight of oxygen per cubic foot of air, the total weight in the given volume is

$$31) \quad \frac{(zyV_{wp} + yC_f V_{wi})(460 + T_c) .308(B_a - B_v)}{(460 + T_c)(460 + T_a)}$$

when volume is converted from volume at  $T_a$  to volume at  $T_c$ , and weight per cubic foot is given at  $T_c$ . This formula represents the total weight of oxygen supplied to any given fire under any conditions, but the effective weight of oxygen may be reduced by displacement of air by products of combustion, as given proportionally by the relation in formulae 29 or 30. Hence, for a general equation giving the total weight of available oxygen in unit time, formula 31 must be multiplied by formula 30, which gives

$$32) \quad \begin{array}{l} \text{Total weight} \\ \text{oxygen} \end{array} = \frac{.308(B_a - B_v)y^2(zV_{wp} + C_f V_{wi})^2(460 + T_c)}{A_c V_r (460 + T_a)^2}$$

The time unit is one second if velocities are given in feet per second, and the total weight of oxygen in any time becomes formula 32 multiplied by  $t$ , the time in seconds.

Formula 32, if applying to the square fire already assumed, becomes

$$33) \quad \begin{array}{l} \text{Total wt.} \\ \text{oxygen} \end{array} = \frac{.308(B_a - B_v)y^2(V_{wp} + 4V_{wi})^2(460 + T_c)\cos s}{(460 + T_a)^2 a^2 \sin^2(s - g)V_{wp}}$$



## Contact

For a given fuel, the amount of air required for complete combustion, or the effectiveness of a given air supply, depends on the perfection of the contact between air and fuel. In an absolute sense, evaluation of the degree of contact is extremely difficult, involving as it does the relative rates of air supply and evolution of combustion products, the position of the burning surface with relation to the air supply, the inter-diffusion of air and volatile combustibles during the exothermic stage of combustion, and contact with charcoal during the later stage of combustion (with the evolution of inflammable CO gas also important), the relative molecular velocities of the substances involved and the effects of contact or catalytic agents. No attempt will be made at present to evaluate absolute contact.

Relatively, it is apparent that the amount of air involved in combustion is proportional to the area of the burning surface. Air is in contact with fuel surfaces not burning but is of no consequence in the combustion process. Due to the fact that combustion cannot occur (theoretically) until all water is driven off from a limited fuel surface, the presence of water in fuels has no direct influence on contact as such, but influences combustion only as the water vapor driven off adds to the products of combustion and thus assists air displacement.

Under static conditions, the contact of air or oxygen with wood fuels may be considered to take place between and to involve very thin adjacent fuel and air layers. In connection with heat relationships to be developed in subsequent reports, the relation

1.47Ab seems quite important. Thus,  
Df

if the wood is pure wood substance (density 1.47), a certain amount of heat will be required to heat the fuel to the ignition point and to a given depth over a fixed unit surface area, and a certain volume of the fuel can be completely burned by a given quantity of air. If, however, the density of the fuel is less than 1.47 (see Table 3), the same quantity of air can combine completely with a larger volume of fuel, and less heat will be required to raise a given surface area to the ignition temperature, since there is less mass of actual wood substance involved for a layer of given depth. Subsequent reports will utilize this relation in detail; its mention here is merely suggestive.



If the air or oxygen supply is zero (entire "air" pressure due to water vapor, for example), obviously no amount of heat, however great, could be sufficient to cause active combustion other than that due to combination of a small part of the fuel constituents with the fuel oxygen, although decomposition and evolution of volatile elements of the fuel undoubtedly would occur. The inception hazard formula therefore must be so constructed as to indicate only the ~~small~~ hazard or combustibility due to fuel oxygen, when air supply is lacking. Under practical conditions, a zero air supply is not likely, although on the Matilija fire of 1932 in Southern California there were large unburned patches where the cover was thick and where the fire in general was most intense. Apparently, these patches were due to the evolution of combustion products at so rapid a rate that air was used up faster than it could be supplied (in view of the extent of the intense fire and the extremely blocked-in nature of the topography), and hence the fire died through lack of oxygen. Other causes may also have been operative, but the foregoing explanation seems soundest in view of the actual circumstances.

It is suggested that relative contact of oxygen or air may be expressed mathematically as follows:

If a unit weight of one pound of standard, dry wood fuel of cubical shape is taken as a reference unit, the volume in cubic feet is given by

$$33a) V_f = \frac{1}{62.428 D_f} = \frac{.01602}{D_f}$$

where 62.428 is the weight of pure water per cubic foot at maximum density (4 deg. C, 39.2 F.). The length of a side of the cube is

$$33b) \left[ \frac{.01602}{D_f} \right]^{1/3} \text{ and the area of a side is}$$

$$33c) \left[ \frac{.01602}{D_f} \right]^{2/3} \text{ and the total surface of the cube is}$$

$$33d) 6 \left[ \frac{.01602}{D_f} \right]^{2/3} \text{ in square feet.}$$

Relatively, the amount of oxygen in contact per square foot of fuel surface is given by the weight of oxygen per cubic foot of air, regardless of the thickness of the layer of air in contact with the fuel. Hence, the relative amount of oxygen in contact with the entire surface of the cube is given by





$$33e) \quad 6 \left[ \frac{.01602}{Df} \right]^{2/3} \left[ \frac{.308(Ba-Bv)}{460+Ti} \right]$$

at the instant of ignition. Ignition being assumed to be instantaneous at the ignition point of 540 F., the rate of supply need not be considered, but merely static layers.

From formula 18, the weight of air required for complete combustion of one pound of standard dry wood fuel is 6.0099 lbs., when the air is dry. The volume of this air, regardless of its water vapor content, at the temperature of ignition, is given by equation 20, approximately, and amounts, very closely, to

$$33f) \quad \frac{4530}{(Ba-Bv)}$$

when computed by constants carried out to a greater number of decimal places than are given in formula 20. Hence, in order for the pound of wood to be completely burned, that number of cubic feet of air must be in contact (relative) with the fuel surfaces. While a pound of fuel is not burned instantaneously at the ignition point, the relative values of all factors remain constant regardless of the actual unit quantity of fuel considered. Therefore, the relative completeness of combustion at the instant of ignition, using a pound of fuel as the unit, is given by

$$33g) \quad \frac{6 \left( \frac{.01602}{Df} \right)^{2/3} \left( \frac{.308(Ba-Bv)}{460+Ti} \right)}{\left( \frac{4530}{(Ba-Bv)} \right) \left( \frac{.308(Ba-Bv)}{460+Ti} \right)}$$

which reduces to

$$33h) \quad \frac{.0000000390655 (Ba-Bv)}{(Df)^{2/3}}$$

eliminating oxygen as such from consideration.

This is merely a relative expression giving

$$\frac{\text{No. cu.ft. air in relative contact}}{\text{No. cu.ft. air required in relative contact for complete combustion}}$$

for a temperature of 540 F., the ignition point.

Application of this relation to the inception hazard formula will be made later.



## The temperature of combustion

During combustion, various products are evolved and heated to a temperature depending on their specific heats, their masses and on the amount of heat evolved by the reaction minus conduction, radiation and convection losses. The products attain a given temperature representative of the convection losses, since they ascend at a more or less rapid rate as a convection or "smoke" column. Besides the factors mentioned, the temperature attained also depends on the speed of the reaction. The convection column cools by expansion and mixing with surrounding air while ascending, and also loses heat by radiation to space and back to the ground, as well as by conduction to the surrounding air. The temperature at the base of the column is closely representative, at least, of the amount of heat being generated by a fire, if the cover and other conditions are more or less uniform, thus making for uniformity in rate and amount of heat lost by the various processes. Under such circumstances, the temperature at the base of the column may be taken to be the fire temperature, with interesting and suggestive results. The actual temperature of the fire or convection column is very difficult to measure under field conditions by the various forms of pyrometers, which are expensive and require more or less skilled handling by persons familiar with the work. To make use of such instruments unnecessary, and yet secure practically accurate values for  $T_c$  (the temperature of the column base), it is suggested that use can be made of various simple relations and a formula derived from them, if measurements are made of

- 1.) Ground slope, measured by clinometer.
- 2.) Slope of the "smoke" column, measured in the same way.
- 3.) The air temperature, measured by thermometer.
- 4.) The wind velocity, measured by anemometer or balloon.

The theory is simple. The actual velocity of ascent of the column may be considered to be the resultant of a vertical component due to the difference in density between the column gases and the outside air, and the wind velocity (ordinarily in a direction parallel to the ground slope, in the lower layers). On level ground, in a calm (except for fire-produced indrafts, usually equal on all sides for a simple unit fire), the column ascends vertically, with an acceleration given by the equation



$$34) \quad a = \frac{g(T'-T)}{T} \quad (\text{Humphreys (11)})$$

In moving air, however, the actual movement of the column may be considered as a resultant  $R$  as in Fig. 5 (page 31a), where  $V_c$  is the vertical column velocity component and  $V_w$  is the prevailing wind velocity, both in the same units. Data are given for various combinations of components, all graphed as vectors, and illustrating the construction of a simple diagram for computing resultants graphically.

On sloping ground, the same considerations apply, assuming that the wind blows parallel to the ground surface, as in Fig. 5a. Knowing the horizontal component of the prevailing wind velocity (the anemometer velocity corrected for instrumental error, since the anemometer, by its nature and plumb exposure, gives a horizontal component directly on sloping ground), the air temperature and the angle or slope between the column and ground, respectively, and the horizontal, the resultant velocity and the vertical component can be calculated, and then the temperature which, in combination with the air temperature, has been the fundamental cause of ascent.

In Humphreys equation for the acceleration  $a$ ,  $g$  is the acceleration of gravity,  $T'$  is the absolute temperature of the column and  $T$  is the absolute temperature of the air, both measured at the same level. This formula, expressed in Fahrenheit degrees and feet becomes

$$35) \quad a = \frac{32.174(T_c - T_a)}{460 + T_a}$$

Velocity in general is equal to  $\frac{1}{2} at$ , and for unit time  $t$ , to  $\frac{1}{2}a$ . Therefore,

$$36) \quad V_c = \frac{16.087(T_c - T_a)}{460 + T_a}$$

which is true only when the composition (and hence the density under standard conditions) of the air and of the gases in the column is identical. If the column gases differ in standard density compared with air, actual density values must be used in the foregoing equations, since temperature alone as used above merely assumes unit (or equal) densities for the two sets of gases.

Since density varies inversely as the absolute temperature (composition the same), the foregoing equations may be expressed by





$$37) \quad V_c = \frac{16.087(D_a - D_c)}{D_c}$$

If  $s\%$  represents the percent of grade or slope (defined as the vertical rise divided by the horizontal distance) of the "smoke" column above (plus) or below (minus) the horizontal, as shown in the figure below,

$$38) \quad V_c = s\% V_w$$

or if the slope is expressed by an angle in degrees,

$$38a) \quad V_c = \tan s V_w$$

Equating 37 and 38a, we have

$$39) \quad \tan s V_w = \frac{16.087(D_a - D_c)}{D_c}$$

for any combinations of air and "smoke" column composition and for level ground only.

Also, for level ground and identical compositions for air and column, we have, from formula 36 and the foregoing:

$$40) \quad T_c = \frac{\tan s V_w (460 + T_a)}{16.087} + T_a$$

and

$$41) \quad V_c = s\% V_w \text{ or } \tan s V_w$$

and

$$42) \quad V_r = \sqrt{V_c^2 + V_w^2}$$

or

$$43) \quad V_r = V_w \sqrt{\tan^2 s + 1}$$

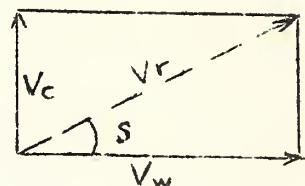
etc. For use in converting velocities in miles per hour to feet per second, the following should be used:

$$44) \quad 1.467 V_{mph} = V_{fps}$$

If  $g\%$  represents the percent slope of the ground above or below the horizontal, it can be shown that

$$45) \quad V_c = V_w (s\% - g\%)$$

and that







$$46) \quad V_r = V_w \sqrt{s\%^2 + 1}$$

and that

$$47) \quad T_c = \frac{V_w(s\% - g\%)(460 + T_a)}{16.087} + T_a$$

for any ground slope, column composition same as air. If angles instead of grade percentage are used, formula 47 becomes

$$48) \quad T_c = \frac{V_w(\tan s - \tan g)(460 + T_a)}{16.087} + T_a$$

Using density (actual) instead of temperature, a general equation for any composition and temperature differences, for ground of any slope, may be secured.

The density of moist air, when referred to dry air at standard conditions as unity, is given by the expression

$$49) \quad D_a = \frac{6.215(2.643B_a - B_v)}{459.6 + T_a}$$

From the percentage composition of the average dry wood, the weight of the products of combustion for incomplete and complete combustion of one pound of the dry wood may be computed from relations already given, resulting in values of approximately 6.991 lbs. for complete and 4.231 lbs. for incomplete combustion, calculated as follows:

Since the percentage by weight of oxygen in a given volume of dry air is 23.2, roughly, the percentage by weight of the remaining gases (termed nitrogen, although there are small quantities of other gases present), is 76.8%.

Combustible	% in 1 lb. fuel	Wt. Prods. per lb. combustible	Products, lbs.
Hydrogen.....	6.06	x 8.94.....	54176 H2O
Carbon.....	49.70	x 3.67.....	1.82399 CO2
Nitrogen in fuel.....	1.05	x 0.0105.....	01050 N2
Nitrogen from air required for combustion; 76.8% x wt. air required or	76.8	x 6.0099.....	4.61560 N2
Ash, incombustible, left behind, 1.89%			

Total wt. products, complete combustion....6.991 lbs.



The total for incomplete combustion is computed similarly, using a value of 2.33 for the weight of products per pound of combustible carbon, instead of 3.67 as for complete combustion (see Table 1), and changing the amount of air required in accordance with formula 19 on page 26.

The virtual densities of the gases in the column as a whole were computed as follows:

Product	% of total wt. of products		Standard* density	Relative Density Contribution
H2O.....	7.75	x	.804 .....	.06231
CO2.....	26.09	x	1.9769.....	.51577
N2.....	66.16	x	1.2568.....	.83150

Virtual density of mixture of products.....1.40958  
for complete combustion, and the density relative to  
air, given by  $\frac{1.40958}{1.2930} = 1.09016$  or about 109% of  
dry air.

Note: \* Density at 32 F., pressure 29.921", in grams per liter..

Similar computations gave a density value for the products of incomplete combustion relative to dry air of 92.45%. It should be noted that water in the fuel (fuel moisture content) when vaporized, adds to the products and decreases the virtual densities. This factor is not included in the foregoing computations.

Thus, the density of the column, with complete combustion and dry fuel, is given by

50)  $D_c = 1.09016 \times \text{air at same temperature and pressure, and}$

51)  $D_c = .9245 \times \text{air at same temperature and pressure,}$

for incomplete combustion.

A formula (49) for the density of air containing any percentage of moisture has already been secured, and substituting density values computed by this formula (modified by values from 50 and 51, above) in formula 39 (with  $\tan s - \tan g \times V_v$  substituted for the left side to take care of ground of any slope), using appropriate temperatures for the column and the air, the formulae for  $T_c$  become



$$52) T_c = .067767V_w(\tan s - \tan g)(460+T_a)+1.09T_a+41.4$$

for any conditions of composition, slope, temperature, relative humidity and wind velocity for complete combustion of standard dry wood fuel of composition given in Table 2, *draft slope of 90° and given wind velocities*

$$53) T_c = .062162V_w(\tan s - \tan g)(460+T_a)+T_a$$

for similar conditions, except that column composition is same as that of the surrounding air, and combustion is not necessarily involved.

$$54) T_c = .057468V_w(\tan s - \tan g)(460+T_a)+.9245T_a-34.7$$

for conditions as in first formula, but for incomplete combustion of standard dry wood fuel.

The implications of this formula of general type for calculating  $T_c$  are rather far reaching. For example, depending on the temperature of the column and of the air, if the fuel is of certain type, the rate of supply of oxygen (and speed of the reaction, other things the same), and the heats lost by convection, conduction and radiation are known, then the heat produced by the fire compared with what should be produced by complete combustion under the given conditions appears to indicate the degree of completeness of combustion. Changes in values of constants in the  $T_c$  formulae occur with changes in the completeness of combustion. At present, the range in values of these formula constants under various conditions varies with a density range of about 16½%. By using the equation for air and column of same densities (53), where doubt exists as to the completeness of combustion, the possible error can be cut to that appropriate to a density range of but 9%.

With practically accurate values for  $T_c$  from the foregoing formulae, it is relatively easy to compute, for example, the indraft velocities that will be produced under various conditions. Although the barometric pressure and the vapor pressure are factors in the density of moist air, they drop out in simplification of the  $T_c$  equations, since both the air and the column are under the air pressure, and the vapor in the air, as the air joins the products of combustion, is the same amount affecting the products of combustion and their virtual density, and hence these factors cancel out.

Besides the problem of determining the completeness of the combustion process in order to use proper constants in the  $T_c$  formulae in individual cases, possible sources of error lie in the following:





- 1.) Use of surface wind velocity, when in fact the velocity usually increases with altitude.
- 2.) Use of surface temperatures, when in fact the velocity of ascent, once the column gases have left the surface, becomes affected by the temperature lapse rate of the air.
- 3.) Use of virtual relative densities at the surface, when in fact changes due to temperature, pressure and mixing occur with altitude.

These errors affect the trend or slopes of the column, primarily. These and other less important sources of error can be kept within reasonable bounds by the following precautions:

- 1.) Use of ceiling or pilot balloons to secure the wind velocity, a vertical angle being taken after one, two or three minutes of flight only, the velocity secured being representative of the average velocity at low elevations (where the angle is measured), and to a limited extent allowing also for lapse rate variations.

- 2.) Not using formulae for narrow, boxed-in canyons where wind eddies and fluctuations are extremely pronounced, or when air is very turbulent for other reasons.

- 3.) Measuring angles only for the lower part of the column, and averaging the minor variations of the column from a straight line.

Most investigators are agreed that definite values for "volume" of heat generated by forest fires under different conditions would be of considerable value, and the formulae given in this report offer a suggestive means for economical and widespread observation of this factor, although the formulae cannot be said to be yet in final form.

#### GENERAL FIRE HAZARD RATING FORMULAE

Although the foregoing does not attempt to give final and complete fire hazard formulae, it is believed to be desirable to indicate how various equations for separate factors may be combined for final ratings. Obviously, the fundamental principle is to combine all factors affecting fire hazard directly, and to divide by all combined factors affecting fire hazard inversely.

It cannot be too strongly emphasized that this preliminary study necessarily goes into considerable detail, but the use of formulae by field personnel is not contemplated. In combining separate equations into a final formula, large sections of the detailed



relations cancel out, and further simplification can be effected by eliminating those factors which prove to be of minor importance. In arriving at final ratings, however, it is desirable to formulate detailed equations on the same principle as that involved in simple arithmetic, where intermediate calculations must be carried to more places than in the answer in order to insure accuracy of the decimal places given in the result. Further, it is likely that final formulae can be expressed adequately by a few pre-computed graphs and tables, making calculation unnecessary, other than minor arithmetical operations.

Inception hazard, in general, may be considered to be adequately expressed for practical fire hazard rating purposes, if the following are known:

1. The heat required to cause ignition.
2. The available relative air supply.
3. The effective heating value of ignition agents.

Expressing the effective heat output of any given igniting agent by the symbol  $HVi$ , without attempt at numerical evaluation, a general formula for inception hazard appears to be the following:

$$55) \quad HI = \frac{1.47 \, HVi \times \text{air supply}}{Df \, HIG}$$

if a unit weight (one pound) of fuel is taken as standard, it is assumed that the heats are applied to unit fuel surface areas (introducing the effects of fuel density, as discussed on page 37), and if pure wood substance (density 1.47) is taken as a reference point for other types of cover. The relative air supply is given by formula 33h. To this must be added the fuel oxygen, since if the air supply were zero, partial combustion still could take place, as already discussed. At the instant of ignition, combustion has just started, and air displacement by products of combustion does not enter the picture. Numerically, the HI formula may now be expressed as follows:

$$56) \quad HI = 1.47 \, HVi \frac{.000000030146 [(Ba-Bv) + 7574351 \, Df^{2/3}]}{Df^{2/3}}$$

---

HIG as in Formula 2, except last element  $SHa(Ti-Ta)Wa$  becomes

$SHa(540-Ta)6.0999 \times$  formula 33h, thus giving relatively the amount of air that must be heated to the ignition point for any given degree of completeness of combustion.



Expressed completely, and simplified, this formula becomes

$$57) \text{ HI} = \text{HVi} \cdot 0.000000044315 \left[ \frac{(\text{Ba}-\text{Bv}) + 7574351 \text{ Df}^{2/3}}{\text{Df}^{2/3}} \right]$$

$$\text{Df} \left[ \text{SHf}(540-\text{Tf}) + 35 + \text{FM}\% \left[ .5(32-\text{Ts}) + 144 \dots \right. \right.$$

$$(\text{cont.}) \dots + (\text{Tb}-\text{Tw}) + \text{Hv} + \text{SHv}(540-\text{Tb}) \left. \right] \dots$$

$$(\text{Cont.}) \dots + \text{SHa}(540-\text{Ta}) \cdot \frac{0.00000023478(\text{Ba}-\text{Bv})}{\text{Df}^{2/3}} \left. \right]$$

The value of the coefficient for the last expression (indicating the amount of heat required to raise air to the ignition point) is merely formula 33h multiplied by 6.0099, the weight of air involved in complete combustion of one pound of fuel. Formula 33h, since it represents the relative completeness of combustion (exclusive of the fuel oxygen), obviously determines the amount of air that must be heated for any given degree of completeness of combustion when thus used as a multiplier of the amount of air required for complete combustion (unity).

The value of formula 33h for use in the numerator as a factor showing relative air supply, obviously must be altered to include the fuel oxygen in similar units so that zero hazard does not occur when air supply is zero. Instead, if the fuel oxygen is added to both the numerator and denominator of formula 33g, under the foregoing conditions a ~~small~~ hazard will be indicated due to partial combustion by reason of fuel oxygen. The steps in deriving the proper numerator coefficient are as follows:

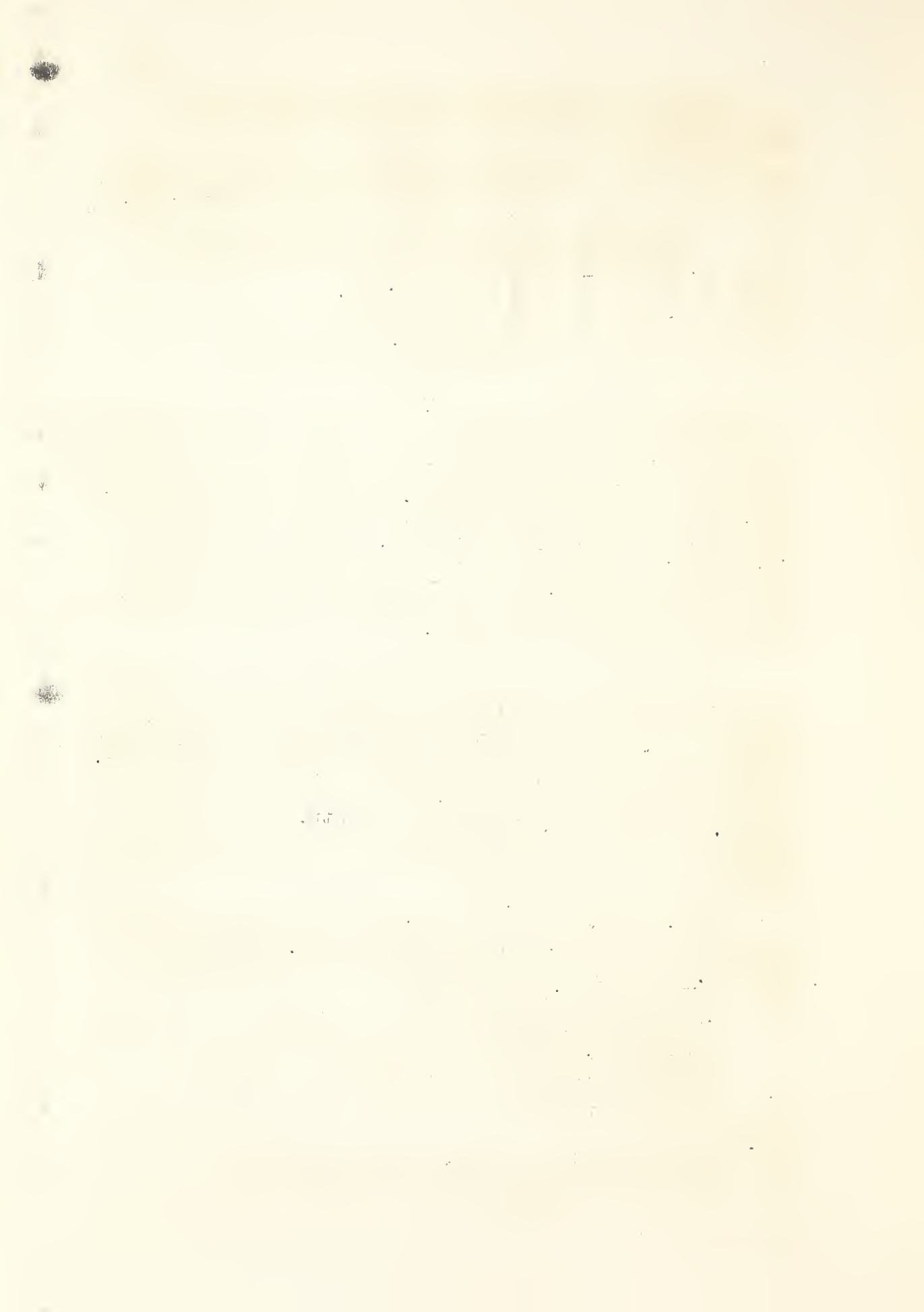
In standard wood fuel, 41.3 % is oxygen, or there is .413 lb. of oxygen per pound of fuel. Hence, the relative degree of completeness of combustion is

$$58) \frac{6(.01602)^{2/3} \cdot .308(\text{Ba}-\text{Bv})}{\text{Df}^{2/3}(460+\text{Ti})} + .413$$

$$\frac{4530(\text{Ba}-\text{Bv}) \cdot .308}{(\text{Ba}-\text{Bv})(460+\text{Ti})} + .413$$

which simplifies to

$$59) \frac{.000000030146 \left[ (\text{Ba}-\text{Bv}) + 7574351 \text{ Df}^{2/3} \right]}{\text{Df}^{2/3}}$$





In formula 57, a value of 540 F. is substituted for the ignition temperature, the specific heat of water is taken as one, a unit weight of fuel is employed, the heat of wetting adopted is the approximate value of 35 Btu per pound for coniferous species found by Dunlap, the heat of fusion is given as 144 Btu, and the relative completeness of combustion as determined by relative air supply is given by suitable coefficients or multipliers. Values for the various temperatures, specific heats and the heat of vaporization indicated by symbols in the formula, will be found in Tables 3, 6 and 7, and in Figure 2.

To illustrate the method of calculation, the following conditions will be assumed:

Ba:29.921" Bv:0" Df: .490 Tf, Ta, Ts:30 FM%:10

With a fuel temperature of 30, the range through which the fuel must be raised is 540-30 or 510 deg. F., and the mean temperature is  $\frac{540+30}{2}$  or 285 F. The mean

specific heat of dry wood at this mean temperature, from Figure 2, is about .41, and the total heat required for the wood is .41 x 510 or 209 Btu. The heat required to overcome the chemical attraction between the wood and its contained moisture is 35 Btu. The fuel moisture is in the form of ice, and hence all stages in the conversion of the fuel moisture to vapor at the ignition temperature must be considered. The specific heat of ice is .5, the temperature range is 32-30 or 2 degrees and the heat required is .5 x 2 = 1 Btu, for one pound of fuel moisture. To this must be added the heat of fusion (melting), amounting to 144 Btu. The boiling point temperature of water at a barometric pressure of 29.921" is 212 F. (from Table 6), and as the temperature of the water (melted ice) is 32 F., the temperature range between the boiling and melting points of water is 212-32 or 180 degrees, and since the mean specific heat of water is approximately 1, the heat required is 1 x 180 or 180 Btu per pound of water. From Table 6, the heat of vaporization at a barometric pressure of 29.921" is 971 Btu. From Figure 2, for a mean temperature of  $\frac{540+212}{2}$  or 376 F., the mean specific heat of

water vapor is about .488, the temperature range is 540-212 or 328 degrees, and the heat involved is .488 x 328 = 160 Btu. All of the foregoing values relating to the fuel moisture must be added together and the sum be multiplied by the fuel moisture percentage (since the latter represents the actual weight of water concerned, rather than the unit pound used in the calculations so far), and hence the heat required for elimination of fuel moisture is





$$(1 + 144 + 180 + 971 + 160) \cdot 10 = 145.6 \text{ Btu}$$

From Figure 2, the mean specific heat of dry air for a mean temperature of  $(540+30)\frac{1}{2}$  or 285 F. is about .24, and as the temperature range is 510, the heat required to raise one pound of air to the ignition point is  $.24 \times 510$  or 122 Btu. However, if combustion completeness is adequately represented by the coefficient already formulated, the actual amount of heat required for the actual amount of air present is

$$122 \left( \frac{.00000023478(Ba-Bv)}{Df^{2/3}} \right)$$

which gives a value of .0000000003 Btu, thus indicating that the air factor in relation to the heat required for ignition need not be considered, and that the coefficient in the denominator of formula 57 and the expression  $SHa(540-Ta)$  should be dropped. Otherwise, the numerical values computed may be totalled as follows:

$$HIG = 209 + 35 + 146 = 390 \text{ Btu.}$$

Inserting this value in formula 57 (see also formula 55), and carrying out the indicated computations, a value for inception hazard is secured:

$$HI = HVi \cdot .0017565$$

Similarly, using assumed conditions identical with the foregoing, but with  $Ta, Tf$  and  $Tw$  100 F. instead of 30 F., the inception hazard is found to be

$$HI = HVi \cdot .0019798$$

If  $HVi$  is not considered, or, rather, the  $HVi$  is the same in both cases, the relative hazard under the second condition of temperature 100 F., compared with that under the first condition of temperature 30F., is

$$\frac{.0019798}{.0017565} = 1.127 \text{ plus, or, in other words,}$$

due solely to a rise in temperature of 70 deg. F. from 30 to 100, the relative hazard increased by 12.7%.

If we assume a temperature of 100, and alter the vapor pressure ( $Bv$ ) to a value corresponding to 100% relative humidity ( $Bv: 1.916$ "), the relative hazard becomes

$$HI = HVi \cdot .0019795, \text{ about, indicating that}$$



relative humidity as such (compare rating of .0019795 with that of .0019798) is of no practical importance in affecting fire inception hazard directly, except as it results in fuel moisture changes. In the given example, the fuel moisture was assumed to remain at 10% in spite of a rise in humidity from zero to 100%. Actually, if the rise in humidity was slow, the fuel moisture would eventually reach an equilibrium value of about 34% (see Figure 1).

These computations also show that, so far as fire INCEPTION is concerned, the variations in air oxygen supply with relative humidity, pressure and altitude, at the ignition temperature of 540 F., are of little consequence. This does not hold for fire TRANSLATION hazard, however, since the temperature generated by the fire may be widely variable under different conditions, the rate of supply is also variable as affected primarily by wind movement, and altitude (or decreased pressure) and displacement by products of combustion produce marked effects. These all lead to considerable fluctuations in the amount of oxygen available for combustion under different conditions. It appears that it is the fuel oxygen that is of primary importance in inception hazard, especially under ordinary circumstances when a normal air supply is present at the instant of ignition.

Formula 57 therefore may be simplified by elimination of the inconsequential elements, and becomes:

$$60) HI = \frac{HVi \cdot .33566}{Df \left[ \left[ SHf(540-Tf) + 35 + Ff \left[ .5(32-Ts) + 144 \dots \right. \right. \right. \\ \left. \left. \left. (cont.) \dots + (Tb-Tw) + Hv + SHv(540-Tb) \right] \right] \right]}$$

giving practically identical results.

This formula is representative of "instantaneous" inception hazard, as distinct from "areal" or "geographical hazard", since time as such is not directly involved (consideration deferred until HVi is evaluated) and comparisons are between unit weights of fuel, and not between the varying quantities of fuel to be found naturally on different unit ground areas. The formula represents theoretical relative hazard of fire inception for

1.) A unit weight (1 lb.) of standard wood fuel with composition as given in Table 2.

2.) A solid fuel in the form of a cube, having a surface area exposed to air and igniting agents appropriate to this shape.





3.) Any species of wood or other solid forest fuel for which good oven dry densities are available.

4.) Any type of cover (if suitable changes in constants are made to allow for variations in fuel shape, surface area, oxygen content and ignition temperature), referred to pure wood substance (density 1.47) as a standard or reference point.

5.) Ignition temperature of 540 F., assumed as fixed and invariable so that it may be used as an index or reference point (fuels of different ignition temperature are not represented by the formula as given, but the formula structure will be identical).

6.) Any air, fuel and fuel moisture temperatures.

7.) Any fuel moisture content.

8.) Any altitude or atmospheric pressure.

9.) Any state of fuel moisture.

10.) Any igniting agent emitting heat considered uniformly distributed over the entire exposed fuel surface, the fuel being of unit weight.

11.) Any degree of insolation (through effects on fuel, fuel moisture and air temperatures).

Expressed more generally, the formula becomes

$$61) HI = \frac{1.47 HVi K}{Df HIG}$$

where K, a constant for any given fuel (nature, shape, exposed surface area, etc.) of unit weight is given by

$$62) K = \frac{Aos Wo + Wfo}{\frac{Face Wo + Wfo}{Ba-Bv}} \quad (\text{see page 21a for symbols})$$

Formulae 60 and 61 compare unit weights of fuel, assumed to be concentrated into a solid block. In nature, however, fuel is distributed over the ground area in numerous individual pieces, hence, for actual geographical or areal (map) ratings, the actual quantity of fuel per unit ground area (horizontal projection) must be used as a multiplier of the formulae in order to compare different unit areas or regions. Satisfactory units for areal ratings would be tons of fuel per square mile, for quantity and area. Over an area, instead of concentrated blocks of fuel of uniform shape, there are very numerous individual pieces of different shapes and sizes, such as twigs, logs, branches, foliage, duff layers and grasses. Thus, if a compact duff layer is to be considered, its exposed surface is practically the area of the actual ground surface (not a horizontal projection, but taking in all irregularities) per square mile (horizontal projection). If the horizontally pro-





jected square mile is used, there would be more actual fuel present per square mile, for a given stand density, on sloping than on level ground, due to greater slope distance. A square mile seems to be a satisfactory unit, but may be translated into other areal units if required. A square foot is not satisfactory since adequate account of the many types and physical forms of forest fuels cannot be taken by so small a sample plot.

It is possible that data collected in connection with the California cover type map can be utilized to secure estimates of quantity of fuel in an areal sense. In estimating the quantity, it will be necessary to employ average density values for the different types of fuels, and in some cases, density values may have to be found from additional laboratory tests by forest agencies (as for some of the brush fuels, grasses, barks and foliage). By approximations, estimates or limited sample plot measurements and observations, it should be possible to approximate the exposed total fuel quantity and surface area for various districts and broad cover type zones. The quantity of fuel obviously affects the chances for ignition in that, other things the same, the probability for ignition varies directly with fuel quantity, no ignition being possible in the absence of fuel. Also, the larger the exposed surface, the better are the chances for ignition. It is apparent that the quantity and surface work in a relative sense, and that while both are directly related to the chances for ignition, in reality they operate as a ratio, which combines the effects of quantity and surface, and tentatively, at least, the foregoing formulae may be multiplied by a coefficient given by

$$\frac{W_f (\text{total})}{S_f (\text{total})}$$

This means that given a heavy fuel of given exposed surface (such as a log), the ignition hazard is much less than the same weight of fuel, but with a much greater surface. This simple ratio is not all that is involved, of course, but at present will be considered as fully meeting practical requirements.

Given the total exposed surface per square mile, the total quantity of fuel in the same area and the heating value per unit weight of fuel, some idea of the "conflagration" hazard may be gained, in conjunction with other formula factors. In other words, a relative measure of the total number of heat units that possibly could be liberated by complete combustion would be gained,



and in connection with weather and miscellaneous factors inserted in a translation hazard formula, the approximate rate of combustion could be found, and hence the relative difficulty of control. It must be borne in mind that precision in formula factor measurements or estimates is neither necessary nor possible, and in any case are not desirable for practical rating work, as precision usually requires too intricate formulae. Periodical examination of a few sample plots should take care of the seasonal and periodic changes in quantity and surface of fuels for current hazard rating purposes (rather than broad general averages for a period of years).

Finally, a general fire inception formula, showing theoretical relative hazard, including the factors just discussed and for any time ( instantaneous, not a period, necessarily) and any area, may be expressed by

$$63) \quad HI = \frac{1.47 \text{ HVi K Aes}(\text{total})}{\text{Df HIG Wf}(\text{total})}$$

Also, formula 60 may be expressed for a compact duff layer instead of a cube as follows (assuming that the top inch of duuf is that primarily involved in fire inception in this type of cover, and that the duff composition is the same as that for standard wood fuel as given in Table 2):

$$64) \quad HI = \frac{\text{HVi} \cdot .33582}{\text{Df HIG}}$$

the changed coefficient .33582 being found from the relation given in formula 58, thus:

$$\frac{\frac{.01602}{.08333 \text{Df}} \cdot \frac{.308(\text{Ba-Bv})}{1000} + .413}{\frac{4530}{\text{Ba-Bv}} \cdot \frac{.308(\text{Ba-Bv})}{1000} + .413} = \frac{.4131}{1.80824} = .22845(x \ 1.47) \dots = .33582$$

where  $\frac{.01602}{\text{Df}} =$  (relative volume of duff weighing 1 lb.)  
 $\frac{.08333}{\text{Df}} =$  (depth of duff layer in feet)

This ratio is equivalent to the first part of the equation just given for computing the coefficient, and is equal to the surface area in square feet of the duff layer. The remainder of the equation represents the relations already discussed, and the result is based on the eliminations of unimportant factors already mentioned.

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It is clear that simple tables and/or graphs can be prepared to make the computations very easy. It is planned to compute tables for a few cover types and fuel conditions for use in checking ratings during the summer work of the mobile fire weather forecasting unit.

### SUMMARY

Definite, approximate relative fire inception hazard rating formulae of theoretical nature have been developed in this report on physical, chemical, and mathematical grounds, employing what appear to be reasonable and logical assumptions where needed for calculation purposes. Some equations for eventual rating of translation hazard have also been developed, but a complete translation hazard formula has not been attempted. The inception hazard formula makes no present attempt at numerical evaluation of the effective heating power of various igniting agents. Granting that the assumptions are sound and the mechanics of calculation correct, whether or not the formulae are strictly correct or sufficiently so for practical purposes depends on the results of detailed and systematic checking against accurate fire, weather and miscellaneous data. Some changes in formula constants or arrangements may be found to be necessary. It is believed, however, that the general results of this study are suggestive of a definite method of attack on the fire hazard rating problem which deals with more or less fundamental aspects of the combustion process as concerned in forest fires, rather than with single isolated factors, important in themselves but not adequate to express fully the ultimate hazard. As further study is completed, additional progress reports will be submitted. A definite program of fire hazard rating study has not been set up; prosecution of such study is incidental to fire weather study in general.

This report gives the results of intermittent field and office work during the past seven years, in connection with general fire weather study carried on as a part of the work of the fire weather service of the U. S. Weather Bureau in fire weather district No. 1 (California and Southwestern Nevada). The report forms a part of the Weather Bureau contribution to the work of the California Region going fire study committee, having as members the Regional Forester, the Director of the California Forest Experiment Station, assigned Experiment Station personnel, the Assistant Regional Forester in charge of Fire Control and the Fire Weather Official of the Weather Bureau.





Strictly, the report is not a duplication of any other study, so far as known; since it employs a divergent (theoretical) method, based primarily on meteorological considerations. The general problem of fire hazard rating, however, is being attacked by forest protection agencies, and pertains primarily to their field of investigation. In general, the methods being followed by these agencies are the experimental and empirical types mentioned earlier in this report. An independent theoretical study thus serves as a desirable and useful mutual check, and may possibly be instrumental in presenting new material.

#### Additional study required

Besides the checking of the relationships given, by comparison with actual fire behavior, it will be necessary for really satisfactory ratings to secure by laboratory tests values for the oven dry densities, chemical compositions and heating values of all of the major types of forest fuels (including woods, barks, foliage, duff and grasses), as well as approximate evaluations of quantity and exposed surface of fuels by surveys of sample plots or otherwise (as from cover type map data), the supplying of these required data being the province of the forest protection agencies. In addition, evaluation of the effective heating value of igniting agents in terms of British thermal units must be attempted, and formulae of general type must be produced for fire translation or spread as well as inception. When and if both inception and translation formulae are available and check with reality, the two probably must be combined in some way, to give a measure of general fire hazard.

It is recommended that formula 64, or this formula with modified coefficients depending on the type and nature of fuel considered, be used in connection with checking against fire data, or for tentative rating of inception hazard, exclusive of the factor of effective heat output of various igniting agents. Until this factor is evaluated, checking may not be said to be complete or adequate.





